**DEVELOPMENT OF A MODIFIED FRUIT FLY OPTIMIZATION ALGORITHM BASED LINEAR QUADRATIC REGULATOR CONTROLLER FOR AIRCRAFT PITCH**

**CONTROL SYSTEM**

**BY**

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**AHMADU BELLO UNIVERSITY, ZARIA**

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**DEVELOPMENT OF A MODIFIED FRUIT FLY OPTIMIZATION ALGORITHM BASED LINEAR QUADRATIC REGULATOR CONTROLLER FOR AIRCRAFT**

**PITCH CONTROL SYSTEM**

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## A DISSERTATION SUBMITTED TO THE SCHOOL OF POSTGRADUATE STUDIES, AHMADU BELLO UNIVERSITY, ZARIA

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## DEPARTMENT OF COMPUTER ENGINEERING FACULTY OF ENGINEERING

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## DECLARATION

I declare that this dissertation titled “**Development of a Modified Fruit Fly Optimization Algorithm Based Linear Quadratic Regulator for the Aircraft Pitch Control System (PCS)**” was carried out by me in the Department of Computer Engineering, Ahmadu Bello University, Zaria as part of the requirements for the award of degree of Master of Science in Control Engineering. All literatures used and cited are duly acknowledged in the reference pages. The information derived from literature has been duly acknowledged in the text and a list of references provided. No part of this dissertation was previously presented for another degree or diploma at this or any other institution.

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| Safiya ALIYU |   |   |
| (Student) | Signature | Date |

## DEDICATION

This research work is dedicated to Almighty Allah (S.W.T), His beloved Prophet Muhammad (S.A.W) and then to my beloved parents.

## CERTIFICATION

This Dissertation titled “DEVELOPMENT OF A MODIFIED FRUIT FLY OPTIMIZATION ALGORITHM BASED LINEAR QUADRATIC REGULATOR CONTROLLER FOR AIRCRAFT PITCH CONTROL SYSTEM” by Safiya ALIYU

meets the regulations governing the award of degree of Master of Science (M.Sc) in Control Engineering of the Ahmadu Bello University, and is approved for its contribution to knowledge and literary presentation.

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## ABSTRACT

This research is aimed at the development of a modified fruit fly optimization algorithm (mFFOA) for the determination of optimized weighting matrices (Q which is a positive definite matrix that penalizes the states and R which is also a positive definite matrix that penalizes the control inputs) of the linear quadratic regulator (LQR) to be used for the aircraft pitch control system (PCS).The standard fruit fly optimization algorithm (FFOA) is an optimization algorithm inspired by intelligent smell and vision behaviour of flies towards fruit. The FFOA suffers from the problem of lack of balance between exploration and exploitation as it has a higher rate of exploitation than exploration leading to a high probability of it being trapped in some local optimal. The mFFOA was developed by modifying the iteration factor of the search radius to a decreasing function to improve the exploration capability of the algorithm and then by introducing a linearly decreasing inertial weight in order to provide an efficient balance between exploration and exploitation of the FFOA. The mFFOA was benchmarked against the FFOA using ten optimization test functions (Ackley, Alpine, Eggcrate, Griewank, Pathologic, Rastrigrin, Rosenbrock, Schaffer, Sphere, and Whitley) and showed a 20% improvement in its convergence to global optima. The optimized values of the Q and R weighting matrices are obtained for ten test runs using mFFOA within a time of 126.9538s when compared with the 140.7819s taken using the FFOA approach. The proposed method reduced the time taken by the FFOA by 13.8281s.These matrices used to determine the LQR controller for the PCS showed a settling time of4.4456s when compared to 4.4764**s** obtained using FFOA. This showed a convergence of the solution search space using the LQR (mFFOA) having a more optimal time-to-solution.

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## LIST OF ABREVIATIONS

ABC Artificial Bee Colony

AFSA Artificial Fish Swarm Algorithm

ANN Artificial Neural Network

ARM Adaptive Radius Mechanism

CI Computational Intelligence

CMAES Covariance Matrix Adaptation Evolution Strategy

CPU Central Processing Unit

DFOA Fruit Fly Optimization Algorithm based on Differential Evolution

EM Electromagnetic

FA Firefly Algorithm

FFO /FOA /FFOA Fruit Fly Optimization Algorithm

FOA-FA Hybridized Fruit Fly Optimization Algorithm and Firefly Algorithm

FOAGRNN FOA-optimized General Regression Neural Network

GA Genetic Algorithm

G-FOA Improved Fruit Fly Optimization Algorithm using Bivariable Function.

GRNN Generalized Regression Neural Network

HP Hewlett-Packard

IFFO Improved Fruit Fly Optimization Algorithm with a new control parameter

JDK Java SE Development Kit

LGMS-FOA Improved Fruit Fly Optimization Algorithm based on Linear

Generation Mechanism of candidate Solution

LQR Linear Quadratic Regulator

MATLAB Matrix Laboratory

mFFOA modified Fruit Fly Optimization Algorithm

MFOA Modified Fruit Fly Optimization Algorithm using random search m and adaptive population size

MIV Mean Impact Value

NLPPs Nonlinear Programming Problems

OLS\_LR Least Squares Linear Regression

PCS Pitch Control System

PID Proportional Integral Derivative

PSO Particle Swarm Optimization

PSOGRNN Generalized Regression Neural Network model with Particle Swarm Optimization

PSOGRNN PSO-optimized General Regression Neural Network

RAM Read Access Memory

RBF Radial Basis Neural Network

RMS Root Mean Square

RMSE Root-Mean-Square Error

SaDE Self-adaptive Differential Evolution Algorithm

SALSSVM Least Squares Support Vector Machine with Simulated Annealing Algorithm

SEDI-FOA Improved Fruit Fly Optimization Algorithm based on Selecting Evolutionary Direction Intelligently

TSP Traveling Salesman Problem

TSPLIB International standard library for Traveling Salesman Problems

wAFSA weighted Artificial Fish Swarm Algorithm

### Background of Research

## CHAPTER ONE INTRODUCTION

The linear quadratic regulator (LQR) is a linear optimal controller which ensures that a feedback control system returns to its state of equilibrium in the presence of disturbances or perturbations. The weighting matrices (Q which is a positive definite matrix that penalizes the states and R which is also a positive definite matrix that penalizes the control inputs) are the critical design parameters for the LQR and are usually selected by the designer ([Hamidi, 2012](#_bookmark8)) which may be time consuming and not necessarily lead to optimal solution. Recently, researches have been carried out for the determination of the optimized weighting matrices of the LQR controller using different computational intelligence (CI) methods which are useful in addressing these issues, such as: genetic algorithm (GA) ( [Nagarkar & Patil, 2016](#_bookmark14) ;[Gupta & Tripathi, 2014](#_bookmark7); [Abdulla *et al.*, 2013](#_bookmark0); Ghoreishi *et al.*, 2011); particle swarm optimization (PSO) (Ghoreishi & Nekoui, 2012; artificial bee colony (ABC) ([Ata & Coban, 2015](#_bookmark2)); weighted artificial fish swarm algorithm (wAFSA) ([Mu’azu *et al.*, 2015](#_bookmark13); [Salawudeen & Mu'azu, 2015](#_bookmark16)), etc. For the purpose of this research work mFFOA is used to determine the weighing matrices of the LQR.

Pan (2011) developed the fruit fly optimization algorithm (FFOA), which is a metaheuristic search method that works based on the food finding behaviour of the fruit fly (*Drosophila*). The main inspiration of FFOA is that the fruit fly is superior to other species in sensing and perception, especially in osphresis and vision it can smell food source 40km away and it has the following advantages: simple structure, immediately accessible for practical applications, ease of implementation and speed to acquire solutions ([Pan *et al.*,](#_bookmark15)

[2014](#_bookmark15)). Studies have shown that it can be used to solve real world and engineering optimization problems ([Pan *et al.*, 2014](#_bookmark15)).

However, the FFOA suffers from the problem of lack of balance between exploration and exploitation in that it has a higher rate of exploitation than exploration leading to a higher probability of it being trapped into some local optimal (Rizk-[Allah, 2016](#_bookmark1)). It also has the drawback of having a fixed value of search radius ([Pan *et al.*, 2014](#_bookmark15)). In order to address these issues, an iteration factor was introduced so that the search radius can be adaptively changed for different evolution phases ([Pan *et al.*, 2014](#_bookmark15)). However, the iteration factor introduced by [Pan *et al.*, (2014](#_bookmark15)) resulted in a larger step size which limits the exploration capability of the algorithm. This work intends to modify the adaptive behaviour of the FFOA by modifying the iteration factor of search radius introduced by ([Pan *et al.*, 2014](#_bookmark15)), to a decreasing function in order to improve the exploration capability and also by introducing a linearly decreasing inertial weight in order to provide an efficient balance between exploration and exploitation of the FFOA.This research aims to apply the modified FFOA (due to its simplicity and its ability to improve the convergence time) to determine the optimized parameters of LQR (Q and R) for the pitch control system (PCS) of an aircraft in order to enhance its time-to-solution.

The PCS helps a pilot to control an aircraft by keeping the pitch attitude constant, that is, make the aircraft return to desired attitude in a reasonable length of time after a disturbance of the pitch angle, or make the pitch follow a given command as fast as possible ([Ju &](#_bookmark11) [Mohamed, 2007](#_bookmark11)). Many research works have been reported on controlling the pitch or longitudinal dynamic of an aircraft for the purpose of flight stability using LQR ([Jisha &](#_bookmark10)

[Aswin, 2015](#_bookmark10); Stefanescu *et al.*, 2013; [Wahid & Hassan, 2012](#_bookmark19); [Wahid & Rahmat, 2010](#_bookmark20)). The approach developed in this work improved the settling time of the PCS.

### Problem Statement

The FFOA lacks balance between exploration and exploitation as such it has higher rate of exploitation than exploration leading to a higher probability of it being trapped into some local optimal. It also has the drawback of having a fixed value of search radius. In order to address this issue, an iteration factor was introduced ([Pan *et al.*, 2014](#_bookmark15)) so that the search radius can be adaptively changed for different evolution phases. However, the iteration factor introduced results in a large step size which limits the exploration capability of the algorithm. Several CI methods have been used to determine the weighting matrices of the LQR controller for complex engineering benchmark system PCS in literature, but these methods require high computational time and are complex.

Thus this research developed an algorithm to determine the weighting matrices of the LQR controller for PCS using decreasing function iteration factor for the search radius to improve the exploration capability of the FFOA and linearly decreasing inertial weight to provide an efficient balance between exploration and exploitation for the FFOA. This improved the time-to-solution in the determination of the mFFOA-based LQR weighting matrices. Also, the effectiveness of the mFFOA-based LQR on the complex PCS system was investigated.

### Aim and Objectives

The aim of this study is to develop a modified fruit fly optimization algorithm (mFFOA) for the determination of the optimized weighting matrices (Q and R) of the LQR controller using the aircraft pitch control system (PCS) as a case study.

In order to achieve this aim, the following objectives were set:

* + 1. Replication of the standard FFOA and development of the modified FFOA by the introduction of a linearly decreasing inertial weight and a decreasing iteration function.
		2. Comparison of the performances of the standard FFOA and the modified FFOA using ten (10) benchmark optimization test functions (Ackley, Alpine, Eggcrate, Griewank, Pathologic, Rastrigrin, Rosenbrock, Schaffer, Sphere, and Whitley) using the convergence to the global optima as the performance metric.
		3. Application of the mFFOA for the determination of the optimized weighting matrices (Q and R) of LQR controller for aircraft PCS model adopted from [Jisha & Aswin](#_bookmark13) [(2015](#_bookmark13)) and evaluating its performance using time-to-solution and settling time.

### Methodology

The methodology adopted for this research work is as follows:

* + 1. Replicate the standard FFOA, using the following steps:
			1. Initialize parameters such as: maximum generation; maximum population; location; step and random reference
			2. Initialize the fruit fly group i.e. random direction and distance of searching for food using the sense of smell of an individual fruit fly.
			3. Generate several fruit flies randomly around the fruit using osphresis for foraging.
			4. Evaluate the population to obtain the smell concentration values (fitness value).
			5. Determine the fruit fly with the maximum smell concentration among the fruit fly swarm.
			6. Retain the best smell concentration value and x, y coordinates, the fruit fly swarm flies toward the position by vision.
		2. Develop the modified FFOA:
			1. Repeat step 1 (a) with random reference =

  min 

 *Iter*max \_ *Iter* 

  max  exp log    







*Iter* 

  max  

max 

where,  is the search radius in each iteration, max is the maximum radius, min is the minimum radius, *Iter* is the iteration number and

*Iter*max is the maximum iteration number.

* + - 1. Repeat step 1(b)
			2. Introduction of linearly decreasing inertial weight

*wk*  *w*max

 *w*max  *w*min  *k*

*iter*

to step 1(c)

max

where, *wk* is the current inertial weigh, *w*max is the maximum generated

inertial weight,

*w*min

is the minimum generated inertial weight and k is

the kth position of inertial weight

* + - 1. Repeat Step 1(d-f)
		1. Compare the performance of the proposed mFFOA with that of the standard FFOA using ten benchmark optimization test functions (Ackley, Alpine, Eggcrate, Griewank, Pathologic, Rastrigrin, Rosenbrock, Schaffer, Sphere, and Whitley)
		2. Determine the optimized LQR weighting matrices (Q and R) using the modified FFOA
		3. Implement the LQR controller obtained in step (4) for the PCS model and evaluate the performance of the PCS performance using settling time and time- to-solution as performance metric when the system is subjected to step signal. All simulations will be carried out in MATLAB R2015a.

### Dissertation Organization

The general introduction of this research has been presented in Chapter One. The remaining chapters are organized as follows: Firstly, a comprehensive review of related literature and important fundamental concepts about Fruit Fly Optimization Algorithm, LQR, PCS, Standard Optimization Test Functions, are carried out in Chapter Two. Secondly, a detailed approach and important mathematical models describing the development of the modified fruit fly optimization algorithm are presented in Chapter Three. Thirdly, the analysis, performance and discussion of the results are shown in Chapter Four. Finally, conclusion and recommendations of further work makes up the Chapter Five. The list of references pertinent to the research and MATLAB codes in the appendices are presented at the end of this dissertation.

## CHAPTER TWO LITERATURE REVIEW

### Introduction

The literature review comprises of the review of fundamental concepts and the review of similar works. In the review of fundamental work, some of the existing works and the fundamental theories of all the algorithms that will be used for the realization of this research are reviewed, and then similar works are reviewed.

### Review of Fundamental Concepts

In this section, concepts fundamental to the research such as: fruit fly optimization algorithm, LQR, and pitch control system of an aircraft, amongst others are reviewed.

### The fruit fly optimization algorithm (FFOA)

Wen-Tsao Pan in 2011 developed a new algorithm known as fruit fly optimization algorithm (FFOA), which was based on the inspiration of the fruit fly, which is superior to other species in sensing and perception, especially in osphresis and vision. They feed chiefly on rotten fruits. In the process of finding food, their osphresis organs smell all kinds of scents in the air, it can even smell food source from 40 km away ([Pan, 2011](#_bookmark33)). They then fly towards the corresponding locations. When they get close to the food locations, they find foods using their visions and then fly towards that direction. FFOA has many advantages such as a simple structure, ease of implementation and speed to acquire solutions. The foraging process of a fruit fly group is shown in Fig. 2.1 ([Li *et al.*, 2013](#_bookmark26) ):



1. The Body Structure (b) Iterative Search for Food Diagram Fig 2.1: Fruit Fly Structure and Search Mechanism ([Li *et al.*, 2013**)**](#_bookmark26)

Despite these advantages, the FFOA however suffers from the problem of lack of balance between exploration and exploitation in that it has a higher rate of exploitation than exploration leading to a higher probability of it being trapped in some local optima (Rizk- [Allah, 2016](#_bookmark1)). It also has the drawback of having a fixed value of search radius ([Pan *et al.*,](#_bookmark15) [2014](#_bookmark15)) leading to poor exploration capability. In order to address this issue, an iteration factor was introduced so that the search radius can be adaptively changed for different evolution phases ([Pan *et al.*, 2014](#_bookmark15)). However, the iteration factor introduced by [Pan *et al.*](#_bookmark15)[(2014](#_bookmark15)) resulted in an increase of step size as the iteration number increases which limits the exploration capability of the algorithm.

The basic FFOA consists of four continuous phases. These are initialization, osphresis foraging, population evaluation, and vision foraging. Firstly, FFOA sets its control parameters, i.e., population size and a finish criterion, and initializes its fruit fly swarm

location. Then FFOA is repeated with the search process of osphresis foraging and vision foraging until the finish criterion is satisfied. At the osphresis foraging phase, a population of fruit flies randomly searches food sources around the fruit fly swarm location. After that, the smell concentration value or fitness value is evaluated for each of the food sources. In the vision foraging phase, the best food source with the maximum smell concentration value is found and then the fruit fly group flies towards it. The mathematical description of FFOA is as follows ([Pan, 2012.](#_bookmark32)):

To implement the FFOA, the following basic steps are used for calculation:

**Step 1**, confirm the fruit fly group’s location by random (X-axis, Y-axis).

**Step 2**, endow personal fruit fly with random value for looking for food and location(X, Y).

X= X-axis+ Random Value; (2.1)

Y= Y-axis+ Random Value. (2.2)

**Step 3**, calculating the personal fruit fly’s distance from the zero point, and find out the S value of density. This value equals to the inverse value of distance.

*Dist* 

*X* 2  *Y* 2 ; *S*  1*dist*

(2.3)

**Step 4**, bring the smell density value S to the density judge function, and find out the smell density value of personal fruit fly at confirmed location. Smell=Function(S).

**Step 5**, repeat step two to step four, calculate the smell density of all the fruit flies in the group, and find the fruit fly with largest and lowest smell density value.

**Step 6**, keep the smell density value and location (X, Y) of the best fruit fly, and the group fly to that location.

**Step 7**, enter in the iterative optimization, and repeat step two to step five, and check whether the smell density value is better than the previous one, if yes, carry on the step six. The flowchart of the FFOA is shown in Fig 2.2 ([Li *et al.*, 2013](#_bookmark25) )

Is gen < max gen ?

 YES

NO

All other swarm fly towards the best location by using their vision

gen =.gen-1

NO

Keep the highest smell function value and update the best swarm location

Stop

Calculate concentration

value (Si) and its smell function (f(Si))Random initialize

Fruitfly swarm

Random initialize

Fruitfly swarm 3\_D location

(X\_axis. Y\_axis. Z\_axis)

 YES

Is pop < max pop ?

Start

Parameter Initialization:

maxgen; maxpop; location; step; random interference

Individual provision of

random direction and distance (Di) for search of food

Fig 2.2: Flowchart of Standard Fruit Fly Optimization Algorithm ([Li *et al.*, 2013](#_bookmark25) )

### Adaptive search radius

The implementation of FFOA basically consists of four (4) major steps. These steps include parameter initialization, osphresis foraging, population evaluation and vision foraging. In the osphresis foraging state, a new solution is evaluated by adding each decision variable of the swarm location and a random value in the range of 1,1 (Pan *et*

*al.*, 2014). This means that, the swarm location of FFOA is rounded within a fixed radius

of 1, which has resulted in an unbalanced behaviour of the FFOA while searching for the optimum solution in a given solution space. For example, at the early stage of the algorithm, the fruit fly swarm location is often far from an optimum solution. Thus, this search radius may be too small and considerable increase in iterations may be required to find a promising region within the solution space. In order to address this, the fixed radius was adaptively changed with iteration factor as introduced in (Pan *et al.*, 2014):

  min 

 *Iter* 

  max  exp log  







*Iter* 

(2.4)

  max  

max 

where  is the search radius in each iteration, max is the maximum radius, min is the

minimum radius, *Iter* is the iteration number and *Iter*max is the maximum iteration number.

The adaptive behaviour given in equation (2.4), significantly improved the performance of

 *Iter* 

the FFOA. However, the 

*Iter*

 iteration factor in equation (2.4) indicates an increasing

 max 

function, this result in a larger step size which limits the exploration capability of the algorithm. Thus, in this research work, the adaptive behaviour in equation (2.4) was

modified to a decreasing iteration function

*Iter*max \_ *Iter* . This decreasing iteration function

*Iter*max

will improve the exploration capability of FFOA.

### Linearly decreasing inertial weight

It has been stated, that, inertial weight strategy provides an efficient balance between exploration and exploitation. Thus, in this research, a linearly decreasing inertial weight was used as it performs better over a large number of optimization problems (Shi & Eberhart, 1999) and is given as:

*wk*  *w*max

* *w*max  *w*min  *k Iter*max

(2.5)

where,

*wk* is the current inertial weigh, *w*max is the maximum generated inertial weight,

*w*min

is the

minimum generated inertial weight and k is the kth position of inertial weight

### Standard optimization test functions

These are standard optimization test functions used to validate the characteristics of optimization algorithms and to compare their various performances ([Li *et al.*, 2013](#_bookmark28)). Many test functions have been reported in literatures, but there is no standard set of test functions needed to be followed. New optimization algorithms should be tested using at least a subset of functions with diverse properties so as to make sure that the tested algorithm can solve certain types of optimization problems efficiently (Tang *et al.*, 2007). In this work, ten (10) test functions will be used to investigate the optimization capability of mFFOA. These test functions have diverse properties to include a wide variety of problems, such as unimodal, multimodal, regular, irregular, separable, non-separable and

multi-dimensional problems(Jamil & Yang, 2013). The test functions considered in this research are described as follows.

1. **Ackley function:** This function is one of the commonly used test function which is continuous, differentiable, non-separable, scalable and multi-modal. The mathematical equation for this function is expressed as follows([Bäck & Schwefel,](#_bookmark3)

[1993](#_bookmark3)):

*f*

 *x*  2*o* exp  1 1 *n*

2   exp  1 *n* cos2 *x*   20  *e*

(2.6)

*Ackley*

 5 *n*

*xi*   *n i* 

 *i*1 

 *i*1 

where

*n*  1, 2,...

and

32.768  *xi*  32.768

for

*i*  1, 2,..., *n* . This function has

global minimum

*f*\*  0 at

*x*\*  (0, 0,..., 0) .

This function has global optimum of

*f* (*x*\* )  0 at

*x*\*  0 for 100  *xi*  100

1. **Alpine function:** Alpine function is continuous, non-Differentiable, separable, non-scalable, and multimodal and is defined as ([Rahnamayan *et al.*, 2007](#_bookmark32)):

*n*

*f* (*x*)   *xi* sin(*xi* )  0.1*xi*

*i*1

This function has global optimum of

*f* (*x*\* )  0 at

*x*\*  0 for 10  *xi*  10

(2.7)

1. **Eggcrate test function:** This function is Continuous, Separable, Non Scalable and is mathematically defined as follows(Yang, 2010c):

*f* (*x*, *y*)  *x*2  *y*2  25(sin2 *x* sin2 *y*)

(2.8)

This function has global minimum of (*x*, *y*) [2 , 2 ][2 , 2 ].

*f*\*  0

occurs at

*x*\*  (0, 0)

in the domain

1. **Griewank test function:** Griewank's function is similar to Rastrigin's function. It has many widespread local minima ([Hansen, 2006](#_bookmark13)). However, the location of the minima are regularly distributed and has the following diverse properties: continuous, differentiable, non-separable, scalable, and multimodal The mathematical expression for this function is as follows ([Fister Jr *et al.*, 2013](#_bookmark6)):

1 *n* 2 *n xi*

*f* (*x*)  4000  *xi*

*i*1

* cos(

*i*1

)  1

*i*

(2.9)

where *n*  1,2,..., and *i*  1,2,..., *n* for  600  *x*  600 **.** This function has a

*i*

global minimum of

*f*\*  0 at *x*\*  (0,0,...0) .

1. **Pathologic function:** Pathologic function is continuous, differentiable, non- separable, non-scalable and multi-modal and is defined as ([Rahnamayan *et al.*,](#_bookmark32)

[2007](#_bookmark32)):

*n*  sin2  100*x*2  *x*2  0.5 2

*f* (*x*)   0.5   *i i*1 



(2.10)

*i*1

1  0.001(*x*2  2*x x*

 *x*2

)2 

 *i i*

*i*1

*i*1 

1. **Rastrigin test function:** Based on the Sphere's function, the Rastrigin's function adds cosine modulation to create many local minima. Because of this feature, the function is multimodal. The mathematical expression for this function is as follows ([Fister *et al.*, 2013](#_bookmark6)):

*f* (*x*)  10*n*  [*x*2 10 cos(2*x* )],

*n*

(2.11)

*i i*

*i*1

This function has global minimum

15  *xi*  15 .

*f*\*  0

at *x*\*  (0,0,...,0) with a constraint of

1. **Rosenbrock test function: :** Rosenbrock's valley is a classic optimization problem, which is also known as Banana function (Tang, K. *et al.*, 2007b). This is continuous, differentiable, non-separable, scalable and unimodal (Jamil & Yang, 2013). The Rosenbrock function is mathematically defined as follows:

*n*1

*f* (*x*)  ((*x* 1) 100(*x*

2

*i i*1

*i*

* *x*2 )2 )

(2.12)

*i*1

This function has global minimum

*f*\*  0

occurs at

*x*\*  (1,1,...,1)

in the

domain of

* 2.048  *xi*  2.048

where *i*  1,2,..., *n* 1. In the 2D case, it is often

written as:

*f* (*x*, *y*)  (*x* 1)2 100( *y*  *x*2 )2

(2.13)

1. **Schaffer function:** Schaffer is a continuous, differentiable, non-separable, non- scalable, multimodal non-convex optimization test function defined as:

  30  2

0.5 

 2 2

0.1 2 

*f x*   *xi*

*i*1

* *xi*1

 sin 50 *xi*



2

* *xi*1 



(2.14)

The Schaffer function has the global minimum domain 100  *xi*  100 ([Li, X. *et al.*, 2013](#_bookmark26))

*f*\*  0 at

*x*\*  0,0,........0in the

1. **Sphere test function:** This is the simplest form of DeJong function. Sphere function is continuous, differentiable, separable, scalable, and multimodal and is mathematically defined as follows ([Schumer & Steiglitz, 1968](#_bookmark34)):

*d*

*f* (*x*)   *x*

2

*i*

*i*1

(2.15)

This function is unimodal and convex with an obvious local minimum of

*f*\*  0 at *x*\*  (0,0,...,0) in a domain of 15  *xi*  15 .

1. **Whitley test function:** Whitley function is continuous, differentiable, separable, scalable, multimodal (Jamil & Yang, 2013) and is mathematically defined as follows (Pan *et al.*, 2014):

*n n*  *y* 2  2 2

*j*

*j*

*k*



*k* 1

  *jk*  cos*y*



*j*1  4000

*jk*

 1 ,





*y jk*

 100*x*

* *x*2 
* 1 *x*2 

(2.16)

with global optimum *x*\*  1,1 ,1and

*f* *x*\*  0 for 100  *x*  100 .

### Linear quadratic regulator (LQR) controller

*i*

The linear quadratic regulator (LQR) is a linear optimal controller that ensures that a feedback control system returns to its state of equilibrium in the presence of disturbances or perturbations. The weighting matrices (Q which is a positive definite matrix that penalizes the states and R which is also a positive definite matrix that penalizes the control inputs) are the critical design parameters for the LQR and are usually selected by the designer ([Hamidi, 2012](#_bookmark8)). The cost function for the LQR, which is the performance index,

is given in:

1   

*J*   *X*

2

*T*

*T*

0

*QX*  *U*

*RU dt*

(2.17)

where J is the cost function, *Q* and *R* are positive-definite Hermitian or real matrices (weighting matrices) used to determine the relative importance of the state variables and

control inputs (expenditure of energy) respectively.

*X T* and *UT* are the transpose matrices

of *X* and *U* (state variables and input function) respectively.

The other parameters, the state and input matrices (A and B), are obtained from the state model of the system.

* + - 1. *Determination of optimal values of weighting matrices in LQR problems*

As stated earlier, the critical design parameters for LQR are the weighting matrices in the objective function (cost function) and are normally selected by the designer. These weighting matrices Q and R have profound effect on controller performance. Determining the best Q and R is usually time-consuming due to its trial-and-error approach requiring several computer iterations and simulations. The LQR is an optimal feedback control approach that minimizes the excursion in state trajectories of a system while requiring minimum control effort ([Cuong *et al.*, 2015).](#_bookmark5) Before the linear quadratic regulator theory is introduced, some definitions that are essential to the theory are presented. Consider the state space representation of a linear time invariant (LTI) system ([Monfort *et al.*, 2015)](#_bookmark28)

.

*x*  *Ax*  *Bu*

*y*  *Cx*  *Du*

(2.18)

(2.19)

where x is an n-dimensional state vector, u is an m-dimensional input vector and y is a p dimensional output vector. A, B, C, and D are constant matrices of the appropriate size. Assuming that, the system is controllable, the LQR approach determines a linear state

feedback law ([Monfort *et al.*, 2015](#_bookmark28) ):

*u*  *Kx*

(2.20)

From equation (2.18) to equation (2.20), the closed-loop system becomes:

.  *A*  *BK* *x*

*X*

(2.21)

and the closed loop eigenvalues are obtained from equation (2.21):

det*I*  *A*  *BK*   0

(2.22)

with the appropriate feedback gain (K), the closed loop poles can be shifted to the desired locations. The optimal control law minimizes the quadratic performance index (cost function) which consists of state and control (inputs) energies as in equation (2.17) ([Cuong](#_bookmark5) [*et al.*, 2015](#_bookmark5)).

A feature of optimal controllers (such as the LQR) is that their introduction to systems will stabilize such systems irrespective of the open-loop stability status. The optimal solution is

the control gain matrix ([Ghoreishi *et al.*, 2011](#_bookmark9) ):

*K*  *R*1*BT P*

(2.23)

Where P is the unique symmetric, positive and semi-definite matrix solution to the

algebraic Riccati equation given as ([Ata & Coban, 2015](#_bookmark3)):

*AP*  *AT P*  *Q*  *PBR* 1*BT P*  0

(2.24)

Equation (2.24) shows that the choice of Q and R will influence P, the solution of the algebraic Riccati equation.

* + - 1. *Methods of determining weighting matrices (Q and R) of LQR*

The problem of selecting weighting matrices has been investigated by several researchers using different methods (standard and intelligent).

### The Standard Methods

In this, normal methods are used to determine the state Q and control R weighting matrices these includes: conventional, Bryson’s, pole placement etc.

1. Conventional Method: Generally, weighting matrices are determined by a trial-and- error method in which an expert adjusts the weighting matrices intuitively, and then refines them iteratively to obtain a satisfying performance. The trial-and-error method is not feasible for high dimensional systems and even for simpler systems; it is labour -intensive and time consuming approach.

Fig 2.3 shows the flowchart for the determination of Q and R using standard method.

End

Yes

Have performance specifications been met?

No

Modify the initial values of Q & R selected

Select initial values of Q & R matrices (positive semi-definite &positive definite matrices respectively)

Performance evaluation of system with the LQR Controller

Obtain the state model of the system

Determine system controllability and observability

Start

Fig 2.3: Flowchart for Determining the Q and R of LQR Controller using Standard Method

1. Bryson’s Method: Bryson’s method ([Johnson & Grimble, 1987](#_bookmark19)) is another iterative method. In this technique, initially, state and feedback variables are normalized with respect to their largest permissible, and utilized to initialize the weighting matrices. Then, similar to trial-and-error method, the weighting matrices are gradually refined to approach the minimum index value.
2. Pole placement Method: This is another popular technique for determining the weighting matrices. However, in pole placement technique; the weighting matrices are based on the given poles, and thus cannot guarantee the performance and constraints of the system.

However, these techniques only aim to minimize the quadratic performance index and control objectives were not considered such as minimizing the overshoot, rise time, settling time, and steady state error. Computational intelligence paradigms have been exploited to enhance the accuracy, design process and performance of the system, and lessen the shortcomings of classic techniques.

### Computational Intelligence Methods

Computational intelligence methods are methods used in solving various problems of artificial intelligence with the use of computers to perform numerous calculations ([Er &](#_bookmark0) [Oentaryo, 2011](#_bookmark0)). These calculations contain the applications of six major techniques: neural networks, fuzzy logic, evolutionary algorithms, rough sets, uncertain variables, and probabilistic methods ([Er & Oentaryo, 2011](#_bookmark0)).

Evolutionary algorithm are inspired from the process of natural evolution([Al-salami,](#_bookmark0) [2009](#_bookmark0)). Among them, are: genetic algorithm (GA), particle swarm optimization (PSO)

algorithm, weighted artificial fish swarm algorithm (wAFSA), artificial bee colony, firefly algorithm, fruit fly optimization algorithm (FFOA) etc.:

* 1. Genetic algorithm (GA): This method ([Haupt & Haupt, 2004](#_bookmark17)) is one of the evolutionary algorithms inspired by natural evolution and it is the most frequent applied algorithm. In GA, the proposed responses for an optimization problem are considered as living creatures. The most important operators and mechanisms used in GA with their equivalencies in nature are:
		1. Selection operator which is equivalent to natural selection phenomenon
		2. Crossover operator which is equivalent to reproduction phenomenon
		3. Mutation operator which is equivalent to genetic mutation phenomenon

By using these operators on current population, new population emerges which is the average of them and not worse than the current population, nevertheless the average is quite often better. Thus, as time goes the GA gives better response for optimization problem.([Abdulla *et al.*, 2013](#_bookmark0); [Ghoreishi *et al.*, 2011](#_bookmark8); and Wongsathan & Sirima, 2009) applied GA to improve the performance of LQR. Although GA is well-founded and indicates high exploration capability, it suffers from two pitfalls: low exploitation and convergence speed.

* 1. Particle swarm optimization (PSO) algorithm: This method was first introduced by James Kennedy and Rassel Eberhart ([Kennedy & Eberhart, 1995](#_bookmark24)). In PSO, a number of simple entities, namely the particles, are placed in the search space of some problem or function, and each evaluates the objective function at its current location. The algorithm, searches a space by adjusting the trajectories of particles as they are conceptualized as moving points in multidimensional space. The

individual particles are drawn stochastically toward the positions of their own previous best performance and the best previous performance of their neighbors. This method is able to reach the globally optimal solution within a few iterations. It has been experimentally shown that the PSO is scalable and its processing time grows at a linear rate with respect to the size of the problem ([Akay, 2013](#_bookmark1)).

* 1. Artificial fish swarm algorithm (AFSA): The basic idea of fish in water is to discover regions with more food, by vision or by sense through its intelligent behaviours (*Preying*, *Swarming* and *chasing)*. Hence the environment where an artificial fish (AF) lives is mainly the solution space of the optimization problem (Wang & Li, 2015) and is usually the state of other fishes.
	2. Weighted artificial fish swarm algorithm (wAFSA) proposed by [Salawudeen &](#_bookmark23) [Mu'azu, (2015](#_bookmark23)) adopted an inertial weight selection such that the algorithm can adaptively select its parameters (visual and step size) when searching for global solution. Crossover operator was applied to fuse the AFSA and the modified cultural artificial fish swarm algorithm (mCAFAC), in order to enhance its convergence to a global minimal. The wAFSA was then applied to determine the optimal values of the weighting matrices (Q and R) of linear quadratic regulator (LQR) controller. This was tested on the quadruple inverted pendulum (QIP) model and was able to stabilize the model in less time compared to using the conventional pole placement LQR and standard AFSA methods.
	3. Artificial Bee Colony (ABC) Algorithm: The ABC algorithm was introduced by Karaboga in 2005. The method is based on the intelligent behavior of honey bee swarms finding nectar and sharing the information of food resources with each

other in the field of swarm intelligence to solve optimize numeric benchmark functions ([Karaboga, 2005.](#_bookmark20)). The general procedure of the ABC algorithm contains four phase; initialization phase, employed bees phase, onlooker bees phase, and scout bees phase. The ABC algorithm has the advantages of strong robustness, fast convergence and high flexibility, fewer control parameters and also it can be used for solving multidimensional and multimodal optimization problems ([Karaboga &](#_bookmark21) [Akay, 2009](#_bookmark21); [Karaboga & Basturk, 2007](#_bookmark22)).

* 1. Firefly algorithm (FA**):** The FA was developed by Xin-She (Yang, 2008) and it is based on idealized behavior of the flashing characteristics of fireflies. For simplicity, we can summarize these flashing characteristics as the following three rules:
		1. All fireflies are unisex, so that one firefly is attracted to other fireflies regardless of their sex.
		2. Attractiveness is proportional to their brightness, thus for any two flashing fireflies, the less bright one will move towards the brighter one. The attractiveness is proportional to the brightness and they both decrease as their distance increases. If no one is brighter than a particular firefly, it will move randomly.
		3. The brightness of a firefly is affected or determined by the landscape of the objective function to be optimized (Yang, 2008).
	2. Fruit fly optimization algorithm (FFOA): The FFOA was developed by Pan in 2011, which works based on the foraging behaviour of the fruit fly on food, the fruit fly is superior to other species in sensing and perception, especially in

osphresis and vision. It has been used to solve real world and engineering optimization problems ([Pan *et al.*, 2014](#_bookmark15)).

For the purpose of this research work mFFOA is used to determine the weighing matrices of the LQR.

### Pitch control system of an aircraft

Pitch is defined as a rotation around the lateral or transverse axis, which is parallel to the wings of an aircraft, and is measured as the angle between the direction of speed in a vertical plane and the horizontal line. The deflection of the elevator brings about changes of pitch, which raises or lowers the nose and tail of the aircraft. When the elevator is raised (defined as negative value), the force of the airflow will push the tail down, thereby causing the nose of the aircraft to rise and the altitude of the aircraft to increase. One of the aims of a pitch control system is to help a pilot to control an aircraft by keeping the pitch attitude constant, that is, make the aircraft return to desired attitude in a reasonable length of time after a disturbance of the pitch angle, or make the pitch follow a given command as fast as possible([Ju & Mohamed, 2007](#_bookmark18)).

The three primary ways through which an aircraft change its direction relative to the passing air is shown in Fig 2.4.



Fig 2.4: Forces, and Moments acting on an Aircraft ([Jisha & Aswin, 2015](#_bookmark12))

Fig 2.4 shows the forces, moments and velocities acting on an aircraft, and the three ways through which an aircraft changes its direction are:

1. Pitch: This is the movement of the aircraft about the lateral axis causing the nose and tail of the aircraft to move up or down.
2. Roll: This is the movement of the aircraft about the longitudinal axis, i.e., the axis which runs along the length of the aircraft
3. Yaw: This is the movement of the aircraft left or right.

**Longitudinal motion:** are those movements through which the aircraft has to move on within the x-z plane and rotation about y-axis (pitch). The three longitudinal equations of motions are derived from the X-force, Z-force and y –moments of an aircraft ([Jisha &](#_bookmark12) [Aswin, 2015](#_bookmark12)) and the pitch control system is shown in Fig 2.5.

*X*  *mg* sin 

 .  *rv*  *qw*

` (2.25)

*m*  *u* 

 

.

.

*M*  *IY q* *I XZ*

*p*2  *r* 2  *rp**I*

 *IZ* 

(2.26)

*Z*  *mg* cos cos 

*X*

 .  *pv*  *qu* 

(2.27)

*m* *w* 

 

Equations (2.25, 2.26 and 2.27) represents the longitudinal (PCS) equations of motions of an aircraft.

where, X and Z is are the aerodynamics force components, p, q and r are the angular velocities along x, y and z axes respectively, u, v and w are the forward(x), pitch (y) and vertical (z) linear velocity and Ѳ, 𝜙 and 𝛿𝑒 represent the orientation of aircraft (pitch angle), roll angle in the earth axis system and elevator deflection angle respectively.



Fig 2.5: Pitch Control System of Aircraft ([Jisha & Aswin, 2015](#_bookmark12))

Fig 2.5 shows the pitch control system of aircraft, where, X𝑏 and 𝑍𝑏 are the aerodynamics force components, p, q and r are the angular velocities along x, y and z axes respectively, u, v and w are the forward(x), pitch (y) and vertical (z) linear velocity and Ѳ, 𝜙 and 𝛿𝑒 represent the orientation of aircraft (pitch angle), roll angle in the earth axis system and elevator deflection angle respectively.

### Performance metrics

The improvement, effectiveness, efficiency, and appropriate levels of internal controls are determined by performance metric of a system (Alagoz *et al.,* 2015).To determine the time response behaviour of the LQR controller, time-domain analysis was carried out.

The response of a dynamic system to an input can be expressed as a function of time. The time response of systems can be calculated if the nature of the input is known and the mathematical model of the system can be determined in time-domain analysis. The time response basically has two components: transient response and the steady-state response.

1. **Transient response**: This is defined as that part of the system response that goes to zero as time goes to infinity and is dependent upon the system poles only and not on the type of input. Therefore, the transient response can be analyzed using a step input. The steady-state response shows where the system output ends as time approaches infinity and depends on system dynamics and the input quantity (Burns, 2001).

The transient-response characteristics of a control system to a unit step input

are identified by the following: Peak overshoot,

*M p* , peak time,

*tp* , settling

time, *ts* , steady-state error,

*ess* , rise time, *tr*

and delay time, *td*

as in Figure 2.6

(Rahim, 2009).



Fig 2.6: Transient Response Characteristics of a System (Rahim, 2009).

* 1. **Delay time (** *td* **):** Time required for the response to reach within 50% of the final steady-state value
	2. **Rise time (** *tr* **):** Time required for the response to rise from 0 to 90% of the final steady-state value
	3. **Peak time (** *tp* **):** Time required for the peak overshoot of the response to occur
	4. **Settling time (** *ts* **):** Time required for the response to reach and stay within

2% to 5% of its final steady-state value.

* 1. **Peak overshoot (** *M p* **):** Normalized difference between the time response peak and the steady output and is defined as:

%*M p*

 *c*(*tp* )  *c*() 100%

*c*()

(2.28)

where *c* *tp*  is the time response peak and c(∞) is the steady output

Equation (2.28) shows how peak/maximum overshoot is calculated from transient response of a system

* 1. **Steady-state error (** *ess* **):** Error between the actual output and desired

output as ‘t’ tends to infinity and is defined as:

*e*  lim[*r*(*t*)  *c*(*t*)]

*ss*

*t* 

(2.29)

where, r(t) and c(t) are the actual input and desired output respectively. Equation (2.29) shows how steady-state-error is calculated from transient response of a system

**Robustness:** This is the low sensitivity to disturbances or perturbations not necessarily considered in the design and analysis of systems. The process/plant dynamics of a robust system can change but, its performance is not expected to weaken to an intolerable level, i.e. the system should be able to bear those effects when executing the tasks for which it was designed. The disturbances and the dynamic behaviour of a system are simulated and analysed using the standard test signals: impulse (sudden shock), step (sudden change), ramp (constant velocity) and parabolic (constant acceleration) as shown in Fig 2.7 (Rahim, 2009).

*r* *t* 

A

*r* *t* 

*r* *t* 

*r* *t*

0 t 0 t 0 t

a) Step b) Ramp c) Parabolic d) Impulse



A

0

1A

t

Fig 2.7: Standard Test signals (Rahim, 2009)

1. **Time-to-solution:** As stated earlier, the conventional method of determining the weighting matrices of LQR (Q and R) is time consuming. In some cases, it may take up to hours or even days before the right combination of this matrices are obtained. In practical system, it is often required that the action of the controller on the system should be as fast and robust as possible since the stability of physical system is of paramount importance.

Though the LQR is an optimal controller, its performance strongly depend on how fast and well the appropriate value of this weighting matrices is able to achieve stability. Therefore, the time to obtain these matrices is crucial and will be employed as a performance metric in this research.

### Review of Similar Works

In this subsection, some of the relevant literatures directly related to the study are reviewed and presented in this section based on two groups: the first part of the review is focused on works based on the modification of the FFOA and the second part is focused on the use of metaheuristics search algorithm to determine the LQR weighting matrices (Q & R).

### Review of Research Works Based on Modification of FFOA

The review of research works done in the area of evolution of the fruit fly optimization algorithm (FFOA) is presented in this section.

**Pan (2011)** presented a new metaheuristic fruit fly optimization-inspired algorithm based on the food finding behavior of the fruit fly. The fruit fly itself is superior to other species in sensing and perception, especially in osphresis and vision. The osphresis organs of fruit flies can find all kinds of scents floating in the air; it can even smell food source from 40 km away. Then, after it gets close to the food location, it can also use its sensitive vision to find food and the company’s flocking location, and fly towards that direction too. The new fruit fly algorithm optimized general regression neural network and multiple regression were adopted to construct a financial distress model for a Taiwan enterprise. The results showed that the RMSE value of the Fruit Fly Optimization Algorithm optimized general regression neural network model had very good convergence classification and prediction capability. However, the algorithm easily got trapped in local optima due to its poor rate of exploration of the solution search space.

[**Li *et al.,* (2013**](#_bookmark29)) proposed a hybrid annual power load forecasting model based on generalized regression neural network with fruit fly optimization algorithm. In this work the generalized regression neural network (GRNN) was used for annual power load forecasting. The FFOA was used automatically to select the appropriate spread parameter value for the GRNN power load forecasting model. The effectiveness of the proposed hybrid model was analyzed using two experiment simulations. The results obtained were compared with some other GRNN hybrids, both showed that the proposed hybrid model

outperforms the GRNN model with default parameter, GRNN model with particle swarm optimization (PSOGRNN), least squares support vector machine with simulated annealing algorithm (SALSSVM), and the ordinary least squares linear regression (OLS\_LR) forecasting models in the annual power load forecasting. However, the algorithm being trapped in local optima due to its poor rate of exploration of the solution search space still existed.

[**Lin (2013**](#_bookmark30)**)** carried out analysis of service satisfaction in web auction logistics service using a combination of Fruit fly optimization algorithm and general regression neural network. In the work fruit fly optimization algorithm (FOA) was adopted to optimize artificial neural network (ANN) model. Principal component regression was carried out on the results data of a questionnaire survey on logistics quality and service satisfaction of online auction sellers to form the logistics quality and service satisfaction detection model. Important principal components in the principal component regression analysis results were selected for independent variables, and overall satisfaction level toward auction sellers’ logistics service as indicated in the questionnaire survey was selected as a dependent variable for sample data. The FOA-optimized general regression neural network (FOAGRNN), PSO-optimized general regression neural network (PSOGRNN), and other data mining techniques for ordinary general regression neural network were used to form a logistics quality and service satisfaction detection model. Four-Six principal components in principal component regression analysis were selected as independent variables of the model. Analysis of the results showed that out of the four data mining techniques, FOA- optimized GRNN model has the best detection capacity. However, this work only applied

the FFOA to optimize the ANN model, the problem of poor exploration capability associated with the FFOA still existed.

[**Xu & Tao (2013a**](#_bookmark27)**)** presented variables screening method based on the algorithm of combining fruit fly optimization algorithm and radial basis neural network (RBF). In their work an RBF neural network was optimized using the standard FFOA and established the network model. This method with mean impact value (MIV) were adopted in variables selection. The strength of this model was tested using two examples. Though the method was found to be, simple to learn, more stable and practical. However, this work only applied the FFOA to optimize the RBF model in variable selection, the problem of the FFOA getting trapped in local optima still existed.

[**Xu & Tao (2013b**](#_bookmark28)**)** proposed an improved fruit fly optimization algorithm using bivariable function. In the proposed modified FFOA (G-FOA) the modification was carried out on the density (S) calculation in order to avoid the limitation of the standard FFOA having a non-negative S value which is not possible in many problems. The performance of the proposed method was tested on three binary nonlinear function using only one classic nonlinear multimode state Rastrigin test function. The results was compared with particle swarm optimization, genetic algorithm and simulated annealing algorithm. The proposed method have the least time-to-solution. However, the problem of fixed search radius still existed.

[**Choubey (2014**](#_bookmark4)**)** proposed fruit fly optimization algorithm for travelling salesperson problem. The work proposed two variants of sensitive smell and three variants for vision functions. The two different variant of the neighborhood search method were proposed for

the implementation of the smell function: Best and Incremental Neighbor Method. The experiment was conducted with JDK 1.6 on an Intel Core™2 CPU with 2.66 GHz and 2 GB RAM. From the experimental results it was found that the smell function best neighbor method converges earlier as compared to the incremental neighbor method. While the sensitive vision function V1 and V3 were found to be comparatively effective in exploration of the search space and finding global optima respectively. The method proposed was applied to the instances of small number of cities. However the work did not consider the problem associated with the fixed search radius of the FFOA as such this problem still existed.

**Iscan & Gunduz (2014)** investigated a constant parameter concerning the direction of the FFO using grid search algorithm. The proposed method automatically adjusted the coefficient for each numeric benchmark function using grid search, and adapted the behavior of the method according to the problem. The performance of the proposed approach was evaluated on optimizing 2 different numeric functions. The experimental results showed that proposed FFO was better than the basic FFO in terms of solution quality. However, the work used the grid search algorithm only as an automated approach for finding the related parameter, as such the unbalanced exploration and exploitation behaviour of the FFOA still existed.

[**Hengyu *et al.,* (2014**](#_bookmark7)**)** proposed an improvement of fruit fly optimization algorithm for solving traveling salesman problems (TSP). The modified algorithm adopted the strategy of adaptive variable step size in order to increase search efficiency effectively. Mutation operator was introduced into the FFOA during the exploration so as to improve the diversity of the population and avoids premature convergence. The performance of the

proposed algorithm was compared with the standard fruit fly optimization algorithm and particle swarm optimization algorithm using nine (9) test functions in TSPLIB international standard library. The simulation results showed that the proposed method performed better. However, the best solution was easily corrupted by the mutation operator which in turn affected the diversification of the solution search space of the proposed algorithm.

**Pan *et al.,* (2014)** proposed improved FFO to solve high-dimensional functions. In the work, the search radius was changed dynamically with iteration number such that the search radius was adjusted for different evolution phases. Weights were generated randomly from a uniform distribution based on the number of points on Pareto fronts, and a weighted sum was used to combine all the objectives into a single objective. A new solution generating method was developed to enhance accuracy and convergence rate of the algorithm. The proposed approach was tested on 30 benchmark functions. The computational results showed that the proposed IFFO not only improved the basic fruit fly optimization algorithm but also performed better than five state-of-the-art harmony search algorithms. However, the work only improved the FFO to solve high-dimensional functions, as such the problem of poor exploration rate of the FFOA still existed.

[**Mhudtongon *et al.,* (2015**](#_bookmark31)**)** proposed modified fruit fly optimization algorithm for analysis of large antenna array. In this work the modified fruit fly optimization algorithm (MFOA) was used to analyze the radiation pattern of the large antenna array. The MFOA was improved by incorporating random search of two groups of swarm and self-adaptive population size feature into the conventional FOA in other to achieve wide search space. The results obtained was tested on three nonlinear test function and the modified

algorithm was found to be effective in solving the three nonlinear test functions and EM problems for the large antenna array. Though the work was able to overcome the problem of getting trapped into local optima, but does not converge to the optimum solution.

**Rizk-Allah (2016)** proposed a hybrid optimization algorithm FOA-FA to solve the nonlinear programming problems (NLPPs) based on FOA and fire fly algorithm. The work integrated the strength of a variation of original fruit fly optimization algorithm (FOA) in handling continuous optimization by employing a new adaptive radius mechanism (ARM) for exploring the whole scope around the fruit flies locations to overcome the drawbacks of original FOA and the merit of firefly algorithm (FA) in achieving robust exploration by updating the previous best locations of fruit flies to avoid premature convergence. The hybrid algorithm speeds up the convergence and improves the algorithm’s performance. The proposed FOA-FA algorithm was tested on eleven benchmark problems and two engineering applications. The experimental simulation result showed that the hybrid algorithm speeds up the convergence and improved the algorithm’s performance. However, the work did not consider the problem of diversification of the solution search space of the FA because it focused on the problem of weak local search ability and premature convergence of the FFO.

[**Wu *et al.,* (2016**](#_bookmark26)**)** proposed an improved fruit fly optimization algorithm (SEDI-FOA), based on selecting evolutionary direction intelligently. In their work a mechanism called selecting the evolutionary direction intelligently was introduced to overcome the problem of random search direction and distance of population individuals. The proposed algorithm was tested on twelve standard benchmark functions and the experimental results showed that the proposed algorithm performed well when compared with some of these extended

FFOA: fruit fly optimization algorithm based on differential evolution (DFOA), improved fruit fly optimization algorithm (IFFO) and improved fruit fly optimization algorithm (LGMS-FOA) and three widely-used evolutionary algorithms: PSO algorithm, the covariance matrix adaptation evolution strategy (CMAES) and the self-adaptive differential evolution (SaDE) algorithm. However, realization of quick convergence in practical problems still existed.

It is evident from the literatures that improving the diversification capability of FFOA has been given a significant research attention leading to the development of the improved algorithms. However, developing a modified FFOA using the concept of modifying the iteration factor of search radius introduced by (Pan *et al.*, 2014) to a decreasing function in order to improve the exploration capability of the FFOA and also introduced a linearly decreasing inertial weight in order to provide an efficient balance between exploration and exploitation of the FFOA was not done to the best of my knowledge.

### Review of Research Works Based on the use of Metaheuristics Search Algorithm for Determination of LQR Weighting Matrices (Q and R)

The review in this section is focused on the use of metaheuristics search algorithms in the determination of LQR weighting matrices (Q and R)

**Ghoreishi& Nekoui (2012)** presented optimal weighting matrices design for LQR based on genetic algorithm and PSO. In this work, some important indices such as closed-loop pole locations, speed of response, and maximum level of control effort were considered and combined into an objective function. The genetic algorithm (GA) and particle swarm

optimization (PSO) were used to solve this problem. The proposed method was applied to a nonlinear flexible robot manipulator model. The results obtained from these algorithms showed that the PSO performed better than the GA. However, this algorithm has higher iteration number as such an algorithm with less computational time will be better.

**Abdulla *et al.,* (2013)** presented genetic algorithm (GA) based optimal feedback control weighting matrices computation. The work attempted to solve the difficulty associated with the selection of the LQR weight matrices using genetic algorithm GA thereby avoiding the trial and error involved in the state feedback technique. The proposed solution was used in the design of position controller of a robot arm. The results obtained showed that the proposed solution satisfied the specifications, for minimum overshoot, settling and rise times. However, it requires higher iterations before reaching the optimal value.

**Ohri (2014)** designed linear quadratic regulator (LQR) and proportional integral derivative (PID) controllers for pitch control system of an aircraft using genetic algorithm (GA) for tuning the parameter of the LQR and PID controllers. The result obtained showed that the PCS with LQR performed better than the PCS with the PID. However, it requires higher iterations before reaching the optimal value.

**Ata & Coban (2015)** presented an artificial bee colony algorithm based linear quadratic optimal controller design for a nonlinear inverted pendulum. The LQR was used to control an inverted pendulum as a nonlinear dynamical system and the Artificial Bee Colony (ABC) algorithm was used for selecting weighting matrices. The result obtained showed that the proposed method performed better than the conventional (trial and error) method. However, this method has the limitations of complexity and high computational time.

**Mu’azu *et al.,* (2015) and Salawudeen & Mu’azu (2015)** proposed weighted artificial fish swarm algorithm with adaptive behaviour based linear controller design for nonlinear inverted pendulum. In this work, first an approach called inertial weight into the standard artificial fish swarm algorithm (AFSA) was introduced to adaptively select its parameters (visual and step sizes) after which, the modified algorithm was used to determine the optimal values of LQR weighting matrices. The proposed method was used to stabilize a non-linear inverted pendulum. The result obtained was efficient in determining the weighting matrices of LQR in comparison with the conventional trial-and error approach. Simulation results showed the efficiency of the method proposed in this work. The complexity of implementing the preying, swarming and chasing behavior of fish is the limitation of this method.

**Nagarkar & Patil (2016)** presented the optimization of the linear quadratic regulator (LQR) control quarter car suspension system using genetic algorithm (GA). In this research, GA was used to determine the optimum weighting matrix parameters of the LQR. A Macpherson strut quarter car suspension system was implemented for ride control application. The GA was implemented with single objective (minimizing root mean square (RMS) controller force) and the analysis was extended to multi-objective optimization with objectives: minimization of RMS controller force and RMS sprung mass acceleration and minimization of RMS controller force, RMS sprung mass acceleration and suspension space deflection. Though the result obtained gave an acceptable value, but the method required a high computational time.

It is evident from the reviewed literatures that several metaheuristic search algorithms have been given relevant research attention leading to their application in the determination of the weighting matrices (Q and R) of LQR for different control engineering benchmark systems. However, the issues of costs still remain valid research areas. In order to address the issues of complexity and high computational time in determining the Q & R of LQR controller associated with most of the reviewed literature, this research developed a modified FFOA that use the concept of linearly decreasing inertial weight for the determination of optimized weighting matrices (Q and R) of LQR for a PCS. The mFFOA reduced the unbalanced behaviour of the FFOA which improved the exploration process of the standard FFOA.

## CHAPTER THREE MATERIALS AND METHODS

### Introduction

In this chapter, the methods, materials and procedures employed for the successful completion of this research are discussed. The standard FFOA and the modified FFOA were replicated and developed respectively.

### Computer System Specification

For each algorithm and for each test case, the best of the ten (10) tests were obtained using MATLABR2015a on Hewlett-Packard HP G62 with an Intel(R) Pentium(R) 2GHz processor and 3GB RAM with 64-bit Windows 7 pro Operating System (OS).

### Initialization of FFOA, LQR and PCS Parameters

As discussed in subsection 2.2.1, the performance of FFOA depends on the appropriate selection of its control parameters (maximum generation, maximum population, location, step, and random interference). The appropriate values selected for these parameters are presented in Table 3.1

Table 3.1: FFOA Simulation Parameters

|  |  |  |
| --- | --- | --- |
| **S/No** | **Simulation Parameters** | **Value** |
| 1 | Population | 1000 |
| 2 | Generation | 50 |
| 3 | Step | Adaptive |

The simulation parameters presented in Table 3.1 are used in determining the performance of the standard algorithm. The MATLAB script for the FFOA algorithm can be found in Appendix B.

The LQR controller used in this research consists of two weighting matrices (Q and R). The Q and R matrices are considered as smell function of the FFOA, performing the ospheresis foraging behaviour of FFOA described in subsection (2.2.1) and are determined using standard methods as shown in Fig 2.3 and equation (2.17).The appropriate values selected for the parameters of the mFFOA used in determining the weighting matrices (Q and R) of the LQR are presented in Table 3.2

Table 3.2: mFFOA (Q and R) Simulation Parameters

|  |  |  |
| --- | --- | --- |
| **S/No** | **Simulation Parameters** | **Value** |
| 1 | Population | 500 |
| 2 | Generation | 50 |
| 3 | Step | Adaptive |

The simulation parameters presented in Table 3.2 are used in determining the weighting matrices (Q and R) of the LQR using the developed algorithm.

The PCS model equations (2.25), (2.26) and (2.27) adopted from ([Jisha & Aswin, 2015](#_bookmark12)) was obtained after substituting the data from the General Aviation airplane.Table 3.3 shows the data from the General Aviation airplane.

Table 3.3: Longitudinal Derivative Stability Parameters ([Jisha & Aswin, 2015](#_bookmark12))

|  |  |  |  |
| --- | --- | --- | --- |
|  |  | **Components** |  |
| Longitudinal Derivatives | **Dynamics Pressure and Dimensional Derivative**Q = 36.8lb/ft2,QS= 6771lb, QS c = 38596ft.lb, ( c / 2u0 ) = 0.016s |
|  | Z-Force, (F-1) | Pitching Moment, ( FT-1) | Pitching Moment, (FT-1) |
| Rolling velocities | *X u* = −0.045 | *Zu* = −0.369 | *Mu* = −0.369 |
| Yawing velocities | *XW* = 0.036*XW* = 0 | *ZW* = −*2.02**XW=0* | *MW* = −0.05*MW* = 0 |
| Angle of attack | *X*α= 0*X*α = 0 | *Zα*= −*355.42**Zα* = *0* | *M*α= −8.8*M*α = −0.8976 |
| Pitching rate | *X a*= 0 | *Za* = *0* | *Ma* = −2.05 |
| Elevator deflection | *X*δ*e*= 0 | *Zδe* = −*28.15* | *M*δ*e* = −11.874 |

To solve the aircraft completely the following model assumptions are made ([Jisha &](#_bookmark12) [Aswin, 2015](#_bookmark12)):

1. The aircraft is steady state cruise at constant altitude and velocity
2. The change in pitch angle does not change the speed of the aircraft under any situation

### Standard Fruit Fly Optimization Algorithm

In this research, the standard FFOA was first replicated as described in Fig 2.2. The ospheresis and vision steps are described in subsection 2.2.1. The MATLAB command implementation of the FFOA is given as in Appendix B.

### Development of the Modified Fruit Fly Optimization Algorithm

As stated earlier, the main shortcoming of the standard FFOA is lack of balance between exploration and exploitation in that it has a higher rate of exploitation than exploration leading to a higher probability of it being trapped in some local optimal and the drawback of having a fixed value of search radius. In order to develop the mFFOA, the following processes were added to the oshphresis foraging step of the standard FFOA: a decreasing iteration factor for an adaptive search radius and a linearly decreasing inertial weight.

### Decreasing iteration function for an adaptive search radius

As discussed in section 2.2.2 an iteration factor was introduced to the fixed search radius so that the search radius can be adaptively changed for different evolution phases given in equation (2.4). However, the iteration factor used resulted to a large step size which limits the exploration capability of the algorithm. In this research, the iteration factor in equation (2.4) was changed to a decreasing function given in equation (2.5) in order to improve the the exploration capability of the standard FFOA and equation (2.4) was modified as:

  



exp log



 min  *Iter*max \_ *Iter* 

(3.1)

max

 10    

*Iter* 

  max   max 

where  is the search radius in each iteration,

max is the maximum radius,

min is the

minimum radius, *Iter* is the iteration number and

*Iter*max is the maximum iteration number.

The iterative function in equation (3.1), ensured that the effect of the fixed radius was reduced by always taking smaller step size as the algorithm moves towards the optimum solution and improved the exploration capability of the standard FFOA.

### Linearly decreasing inertial weight

As discussed in section (2.2.3) this was introduced to the Ospheresis stage of the FFOA in order to have an efficient balance between exploration and exploitation that is the decreasing iteration function was substituted in equation (2.4) and used to determine the contribution of the previous fruit fly position to the fruit fly position in the current time step. The MATLAB code description of the modified algorithm is given in Appendix A. Based on the MATLAB code in Appendix A, the flow chart implementation is presented in Fig 3.1:

All other swarm fly towards the best location by using their vision

gen=.gen-1

Stop

Individual provision of

random direction and

distance(Di ) for search of food

Parameter Initializatio:n

maxgen; maxpop; location; step; random interference

Start

Apply Linear Weight

Is pop < max pop?

YES

Random initialize Fruitfly swarm 3\_ D location

(X\_axis. Y\_axis. Z\_axis)

NO

Apply Linear Weight

NO

Keep the highest smell function value and update the best swarm location

Calculate concentration value(Si ) and its smell function(f(Si )) Random

initialize

Fruitfly swarm

Is gen< max gen?

YES

Fig 3.1: Modified FFOA Flowchart

Fig 3.1 shows the flowchart for the modified FFOA. From Fig 3.1, it can be observed that the contribution of the previous fruit fly position to the fruit fly position in the current time step, reduced the unbalanced exploitation and exploration behaviour of the standard FFOA given in Fig. 2.2.

### Performance Evaluation

The performance of the standard and modified FFOA was evaluated using performance metrics listed in subsection 2.2.4

### Comparison of the Results obtained from the Developed Modified FFOA with the Results of the Standard FFOA

The results obtained from the developed modified algorithm were compared with that of the replicated FFOA. The MATLAB code for the comparison is found in Appendix C.

### Determination of Weighting Matrices Using mFFOA

The mFFOA developed in this research is used for the determination of optimized values of the weighting matrices (Q and R) of LQR controller. The most important points in Q and R matrices are the constraints on them. As mentioned in subsection 2.2.5, the Q and R matrices should be positive and semi-definite and positive and definite respectively. However, these constraints cannot be achieved easily. A simple relationship between matrix elements and their positive definiteness is indescribable. It is known that for any real symmetric matrix *N* is positive definite if there exists a real [nonsingular matrix](http://mathworld.wolfram.com/NonsingularMatrix.html) *M* , *N*  *M T M* is nonnegative, i.e., it can be said that matrix *N* is positive definite (Ayres 1962). Thus, in this research, mFFOA is used to first find the optimized values of *L* and

*K* , then *Q* and *R* matrices are calculated as:

*Q*  *LT L*

(3.2)

*R*  *KT K*

(3.3)

Equations (3.2) and (3.3) is used to make Q and R positive semi-definite matrices. (Wang *et al*., 2014). This method was used in this research to make initial responses and to code the responses of the problem. The matrices *J* and *K* which satisfies equations (3.2) and (3.3) are used instead of using Q and R matrices as unknown variables.

Then the corresponding cost function given in equation (2.17) becomes

*J*  *x q xT*  *x q xT*  *x q xT*  *u ruT*  *dt*



(3.4)

 1 1 1

0

2 2 2 3 3 3

In this case, *n* represent the size of the matrix, which in this work is the matrix of pitch control (*n=*3), J represent the cost function, *q* and *r* are weighting matrices used to determine the relative importance of the state variables and control inputs respectively.

*T*

*x*

1 *n*

and *uT* are the transpose matrices of

*x* 1 *n* and *u* (state variables and input function)

respectively.

The MATLAB code for the determination of the weighting matrices of LQR using mFFOA is given in Appendix A:

Based on the MATLAB code in Appendix A, the flow chart implementation is presented in Fig. 3.2.



Fig 3.2: Flowchart for the Determination of Optimized Q and R using mFFOA

Fig 3.2 shows the flowchart for the determination of optimized weighting matrices (Q & R) of the LQR using mFFOA. At the initial stage, the state model of the pitch control system is inputted and control test was performed to establish the controllability and observability of the system. Then, an initial value is randomly assigned to the weighting matrices (satisfying constraints) and the cost function value is evaluated. If the optimum cost is obtained, the values of Q and R which produce that cost is selected as the optimized values of the weighting matrices. Otherwise the values of Q and R are adjusted using the mFFOA or the FFOA depending on the algorithm to be run. Then the value Q and R are

updated and the cost function is evaluated again. This procedure is repeated until the optimum cost is obtained.

### Pitch Control System Stabilization

The linearized state space model adopted from [Jisha & Aswin (2015](file://localhost/C%3A/Users/SAFIYYA/Downloads/SAFIYA_THESIS_v9ff.docx%23_ENREF_18))for the PCS of an aircraft was obtained by linearizing (using small-signal disturbance theory) equations (2.26) to (2.28), and substituting the data in Table 3.2 is given as follows ([Jisha & Aswin,](file://localhost/C%3A/Users/SAFIYYA/Downloads/SAFIYA_THESIS_v9ff.docx%23_ENREF_18)

[2015](file://localhost/C%3A/Users/SAFIYYA/Downloads/SAFIYA_THESIS_v9ff.docx%23_ENREF_18)):

 . 

  

  2.02

1 0 

 0.16 

 .    6.9868  2.9476 0 *q*   11.7304*e*

(3.5)

*q*     

 . 

  0

1 0   0 

   

 

   

*y*  0 0 1 *q*   0*e*

(3.6)

 

 

Equations (3.5) and (3.6) show the state space model of the PCS which corresponds to the standard state space model representation described in equations (2.18) and (2.19) respectively.

Where,

 . 



 

.  .

*x*  *q* 

(3.7)

 . 

 

  2.02 1 0

*A*   6.9868  2.9476 



0



(3.8)

 0 1 0

 

*x*   *q* 

(3.9)

 

 

 0.16 

*B*  11.7304

(3.10)

 

 0 

*u*  *e*

(3.11)

Equations (3.8) and (3.10) are the state and input matrices respectively of the PCS model where  , *q* ,  and *e* are angle of attack, pitch rate, pitch angle and elevator deflection angle.

Furthermore, a few of design specification have to be set to investigate the performance of the control strategies using both mFFOA and FFOA algorithms to determine the Q and R of the LQR which was applied to the PCS. In this work, two considerations have to be met which are settling time specification of PCS less than 5 second and time to solution less than 150 second so as to achieve fast control.

Control test was performed to determine the controllability and observability of the system (PCS), before the mFFOA is used to obtain the Q and R weighting matrices. The MATLAB command of the control test code is given as follows:

% Determine Controllability and Observability of PCS OBV=obsv(A,C);

CTR=ctrb(A,B);

R\_OBV=rank(OBV) R\_CTR=rank(CTR)

if rank(CTR)==size(A) 'System is Controllable'

else

'System is NOT Controllable'

end

if rank(OBV)==size(A) 'System is Observable'

else

'System is NOT observable'

end

A snippet of the output from the above program is given as in Fig 3.3:



Fig 3.3: A Snippet of the Output for Controllability and Observability Test Program From Fig 3.3 it is evident that the state controllability and observability of the system are in full rank. Hence the closed loop poles can then be initialized anywhere in the left-hand side of the complex s-plane. This assertion is necessary in order to establish that the model can be stabilized before designing the controller. First, a program is written to determine the initial positions of the eigenvalues as follows:

function [Q R K P E eigenvalue kk]=lqrQR(A,B) [a1,a2]=size(A);

[b1,b2]=size(B); eigenvalue=eye(a1); for i=1:a1;

realeigen=-1\*rand;

imageigen=randi(5,1)\*rand\*((min(min(A))+max(max(A))\*(rand\*ma x(max(A))\*100)^0.125)\*max(max(B)))^0.5;

eigenvalue(i,i)=realeigen+1i\*(-1)^i\*imageigen;

end

where A and B are the state and input matrices obtained from the linearized LQR model ([Jisha & Aswin, 2015](file://localhost/C%3A/Users/SAFIYYA/Downloads/SAFIYA_THESIS_v9ff.docx%23_ENREF_18)).

To determine the appropriate gain that satisfies the locations of the poles, equation (2.22) was used and mFFOA is randomly used to determine the optimized values of Q and R which satisfies equations (3.2) and (3.3) respectively. The complete program can be found in Appendix A. The fitness function is called from program in Appendix A (mFFOA) using the following code:

if testfunction ==0

A=input('Please Enter The A matrix:\n Such That:\n dx/dt=Ax(t)+Bu(t).\n\nA = ');

clc

B=input('Please Enter The B matrix:\n Such That:\n dx/dt=Ax(t)+Bu(t).\n\nB = ');

clc t=0;

while t<QR\_Iteration [Q,R]=lqrQR(A,B)

t=t+1; end

The stability of the system using the optimized values of the mFFOA weighting matrices Q and R was confirmed using the pole zero map plot (pzmap) in MATLAB as shown in Fig3.3.

[KmFOA PmFOA EmFOA]=lqr(A,B,Q\_mFOA,R\_mFOA)%Q and R used here are obtained from mFOA

sys\_LQmFOA =ss(A-B\*KmFOA ,B,C,D);

pzmap(sys\_LQmFOA) sgrid



Fig 3.4 Pole-Zero Map of the PCS

Fig 3.4 shows the locations of the eigenvalues in the complex s-plane. It is clear that all the eigenvalues (marked ‘x’) are on the negative half of the complex s-plane, thereby, indicating stability.

Step-by-step approach for determining the Q and R weighting matrices are as follows.

1. Initialize all the parameters of the mFFOA
2. Define the problem by specifying A, B and initialize the pole location
3. Provide an initial guess for L and K.
4. Calculate Q and R from equations (3.2) and (3.3) respectively using mFFOA
5. Repeat step 4 until the best value of Q and R is obtained
6. Solve the Riccati equation (2.24) and determine the gain matrix K equation (2.23).

The block diagram of the PCS system with the LQR controller whose weighting matrices are obtained using the mFFOA is as shown in Fig. 3.5.



Fig 3.5: Block Diagram of the PCS with the mFFOA-Based LQR

Fig 3.4 shows the implementation of the modified FFOA based LQR optimized weighting matrices (Q & R) on the PCS. The optimized values of Q and R, are determined using the smell and vision intelligent behaviour of fruit fly towards fruits. The MATLAB code for the step response of the PCS with the mFFOA-Based LQR can be found in Appendix C.

* 1. **Introduction**

## CHAPTER FOUR RESULTS AND DISCUSSIONS

In this chapter, the performances of the modified FFOA are evaluated using the optimization test functions discussed in subsection 2.2.4. Two dimensional (2D) plots were presented for the understanding of all the test function. The performances of the proposed algorithm was compared with the performance of the replicated standard FFOA for validation. The LQR weighting matrices determined using mFFOA and the responses of the PCS were also presented.

### Performance evaluation of mFFOA on the Optimization Test Function

First the standard Fruit Fly Optimization Algorithm was replicated. The performance of the replicated FFOA was evaluated using ten optimization test functions selected for the purpose of this research work, the MATLAB code used for the evaluation is found in Appendix A and the result is compared with the result obtained using the mFFOA found in Appendix B. The results are shown in Table 4.1

Table 4.1: Results obtained for mFFOA, FFOA and Global for the Ten Optimization Test Functions.

|  |  |  |  |  |
| --- | --- | --- | --- | --- |
| SN | Test Function | FFOA | mFFOA | Global |
| 1 | Ackley | 0.0034 | **0.0003** | 0.0000 |
| 2 | Alpine | 0.0001 | 0.0001 | 0.0000 |
| 3 | Eggcrate | 0.0000 | 0.0000 | 0.0000 |
| 4 | Grienwank | 1.0000 | 1.0000 | 0.0000 |
| 5 | Pathologic | 0.0000 | 0.0000 | 0.0000 |
| 6 | Rastrigin | 0.0001 | 0.0001 | 0.0000 |
| 7 | Rosenbrock | 0.0000 | 0.0000 | 0.0000 |
| 8 | Schaffer | 0.0000 | 0.0000 | 0.0000 |
| 9 | Sphere | 0.0000 | 0.0000 | 0.0000 |
| 10 | Whitely | 0.4600 | **0.0000** | 0.0000 |

It is clear from Table 4.1, that, mFFOA outperformed the FFOA on ackley test function and Whitely (as indicated in bold) indicating a 20% improvement. Whereas, both algorithm obtained the same solution which is equal or approximate to the global value in the (7) test functions indicating 70% of the test functions. The superiority of mFFOA over FFOA is expected since a decreasing inertial weight was introduced which provided a much better balance between exploration and exploitation thereby reducing the ability of the algorithm being trapped into some local optimal.

In order to show the optimization process of both the algorithms the minimization plot (fitness/smell function plot) was generated usingMATLAB commands. Figs. 4.1 to 4.10 show the superimposed plots for the mFFOA and FFOA on the minimization plots for the test functions used for the purpose of this research.

### Ackley function

The superimposed minimization plot for Ackley function using the mFFOA and the standard FFOA is as shown in Fig 4.1.

**Ackley Cost Minimization**

**0.8**

**mFFOA**

**FFOA**

**0.7**

**0.6**

**0.5**

**Best Cost**

**0.4**

**0.3**

**0.2**

**0.1**

**0**

**0 100 200 300 400 500 600 700 800 900 1000**

**Iteration**

Fig 4.1: mFFOA and FFOA Ackley Cost Minimization Process

From Fig 4.1, it is clear that both mFFOA and FFOA minimize the Ackley function efficiently to a value of 0.0003 and 0.0034 respectively which is the optimum value both can obtain for the function. Thereafter, the result remains constant throughout the optimization process.

### Alpine function

The superimposed minimization plot for Alpine function using the mFFOA and the standard FFOA is as shown in Fig 4.2.

**Alpine Cost Minimization**

**0.03**

**mFFOA**

**FFOA**

**0.025**

**0.02**

**0.015**

**Best Cost**

**0.01**

**0.005**

**0**

**0 100 200 300 400 500 600 700 800 900 1000**

**Iteration**

Fig 4.2: mFFOA and FFOA Alpine Cost Minimization Process

From Fig 4.2, it is clear that both mFFOA and FFOA minimize the Alpine function efficiently to a value of 0.0001 and 0.0001 respectively. Thereafter, the result remain constants throughout the optimization process.

### Eggcrate function

The superimposed minimization plot for Eggcrate function using the mFFOA and the standard FFOA is as shown in Fig 4.3.

**Eggcrate Cost Minimization**

**0.7**

**mFFOA**

**FFOA**

**0.6**

**0.5**

**0.4**

**Best Cost**

**0.3**

**0.2**

**0.1**

**0**

**0 100 200 300 400 500 600 700 800 900 1000**

**Iteration**

Fig 4.3: mFFOA and FFOA Eggcrate Cost Minimization Process

From Fig 4.3, it is clear that both mFFOA and FFOA minimize the Eggcrate function efficiently to a value of 0 and 0 respectively. This remains constant throughout the optimization process.

### Grienwank function

The superimposed minimization plot for Grienwank function using the mFFOA and the standard FFOA is as shown in Fig 4.4

**Griewank Cost Minimization**

**1**

**mFFOA**

**FFOA**

**1**

**1**

**1**

**Best Cost**

**1**

**1**

**1**

**1**

**1**

**0 100 200 300 400 500 600 700 800 900 1000**

**Iteration**

Fig 4.4: mFFOA and FFOA Grienwank Cost Minimization Process

From Fig 4.4, it is clear that both mFFOA and FFOA for the Grienwangk function got trapped into some local optima to a value of 1, whereas the global optimal solution is a value of 0.

### Pathologic function

The superimposed minimization plot for Pathologic function using the mFFOA and the standard FFOA is as shown in Fig 4.5.

**Pathologic Cost Minimization**

**1**

**mFFOA**

**FFOA**

**0.8**

**0.6**

**0.4**

**0.2**

**Best Cost**

**0**

**-0.2**

**-0.4**

**-0.6**

**-0.8**

**-1**

**0 100 200 300 400 500 600 700 800 900 1000**

**Iteration**

Fig 4.5: mFFOA and FFOA Pathologic Cost Minimization Process

From Fig 4.5, it is clear that both mFFOA and FFOA minimize the Pathologic function efficiently to a value of 0 and 0 respectively. This remains constant throughout the optimization process.

### Rastrigin function

The superimposed minimization plot forRastrigin function using the mFFOA and the standard FFOA is as shown in Fig 4.6.

**Rastragin Cost Minimization**

**1.5**

**mFFOA**

**FFOA**

**1**

**Best Cost**

**0.5**

**0**

**0 100 200 300 400 500 600 700 800 900 1000**

**Iteration**

Fig 4.6: mFFOA and FFOA Rastrigin Cost Minimization Process

From Fig 4.6, it is clear that both mFFOA and FFOA minimize theRastrigin function efficiently to a value of 0.0001 and 0.0001 respectively. Thereafter, the result remains constant throughout the optimization process.

### Rosenbrock function

The superimposed minimization plot for Rosenbrock function using the mFFOA and the standard FFOA is as shown in Fig 4.7.

**Rosenbrock Cost Minimization**

**1**

**mFFOA**

**FFOA**

**0.8**

**0.6**

**0.4**

**0.2**

**Best Cost**

**0**

**-0.2**

**-0.4**

**-0.6**

**-0.8**

**-1**

**0 100 200 300 400 500 600 700 800 900 1000**

**Iteration**

Fig 4.7: mFFOA and FFOA Rosenbrock Cost Minimization Process

From Fig 4.7, it is clear that both mFFOA and FFOA minimize the Pathologic function efficiently to a value of 0 and 0 respectively. This remains constant throughout the optimization process.

### Schaffer function

The superimposed minimization plot for Schaffer functionusing the mFFOA and the standard FFOA is as shown in Fig 4.8.

**Schaffer Cost Minimization**

**1**

**mFFOA**

**FFOA**

**0.8**

**0.6**

**0.4**

**0.2**

**Best Cost**

**0**

**-0.2**

**-0.4**

**-0.6**

**-0.8**

**-1**

**0 100 200 300 400 500 600 700 800 900 1000**

**Iteration**

Fig 4.8: mFFOA and FFOA Schaffer Cost Minimization Process

From Fig 4.8, it is clear that both mFFOA and FFOA minimize the Schaffer function efficiently to a value of 0 and 0 respectively. This remains constant throughout the optimization process.

### Sphere function

The superimposed minimization plot for Sphere functionusing the mFFOA and the standard FFOA is as shown in Fig 4.9.

**Sphere Cost Minimization**

**0.02**

**mFFOA**

**FFOA**

**0.018**

**0.016**

**0.014**

**0.012**

**Best Cost**

**0.01**

**0.008**

**0.006**

**0.004**

**0.002**

**0**

**0 100 200 300 400 500 600 700 800 900 1000**

**Iteration**

Fig 4.9: mFFOA and FFOA Sphere Cost Minimization Process

From Fig 4.9, it is clear that both mFFOA and FFOA minimize the Sphere function efficiently to a value of 0 and 0 respectively. Thereafter, the result remains constant throughout the optimization process.

### Whitely function

The superimposed minimization plot for Whitely function using the mFFOA and the standard FFOA is as shown in Fig 4.10.

**Whitely Cost Minimization**

**1.4**

**mFFOA**

**FFOA**

**1.2**

**1**

**0.8**

**Best Cost**

**0.6**

**0.4**

**0.2**

**0**

**0 100 200 300 400 500 600 700 800 900 1000**

**Iteration**

Fig 4.10: mFFOA and FFOA Whitely Cost Minimization Process

From Fig 4.10, it is clear that both mFFOA minimize the Whitely function efficiently to a value of 0 whereas the FFOA got trapped into local optima to a value of 0.46. The results from each of the algorithm remains constant throughout the optimization process.

### Application of the Developed mFFOA Based LQR Controller for Optimal Determination of Controller Parameters

In order to determine the efficiency of the mFFOA in determining the weighting matrices of the LQR controller, both algorithms were ran ten times due to the stochasticity of the algorithm. The optimized Q and R obtained for the mFFOA and FFOA were tabulated as in Table 4.2.

Table 4.2: Comparison of the Q and R Matrices for mFFOA and FFOA

|  |  |  |  |  |
| --- | --- | --- | --- | --- |
|  | **mFFOA** |  | **FFOA** |  |
| Runs: | Q | R | Q | R |
| 1 |  5.2741 0.0467 0.0196  | 0.4181 | 6.8266 0 0.0164  | 0.1308 |
| 2 | 13.5825 0 0   |  |  6.1389 0.0120 0.0446  |  |
|  | 0.5656 | 0.2504 |
| 3 | 10.0585 0 0.04249  | 0.2273 |  9.5549 0.06310 0.0307   | 0.2701 |
| 4 |  |  |
|  3.2476 0 0   |  | 6.8266 0 0.0164  |  |
|  | 0.1615 | 0.1308 |
| 5 |  |  |
| 27.7918 0.0163 0.0588  27.5803 0 0.0583  24.5498 0.0233 0  4.5631 0 0  16.5461 0 0.0346  21.6173 0.0277 0   |  |  6.1389 0.0120 0.0446 9.5549 0.0631 0.0307 9.5890 0 0.0319 0 9.6145 0.0319 0.9990 0 0  0.6832 0 0.0011 0 0.6796 0 17.4394 0 0  0 17.3370 0.0235  |  |
|  | 0.2898 | 0.2504 |
| 6 |  |  |
|  | 0.2944 |  |
| 7 |  | 0.2701 |
| 8 | 0.1978 | 0.1484 |
| 9 | 0.1630 | 0.3138 |
|  | 0.2374 |  |
|  |  | 0.2409 |
| 10 |  |  |
|  | 0.2953 |  |
|  |  | 0.4884 |

Table 4.2 shows the values of the optimized weighting matrices (Q and R) of the LQR controller using the mFFOA and FFOA. From the result it is clear that the mFFOA gives better optimized values of Q’s and R’smatrices which was able to stabilize the PCS system with a settling time less than that of the PCS design specification in seven (7) out of the ten

(10) runs. The settling time (ts) was obtained from the step response analysis of the LQR, which stabilizes the PCS using the MATLAB code in Appendix C by changing the Q and R values from first to the tenth run. The time taken to determine the weighting matrices were calculated as the time-to-solution/elapsed time (t2s) using MATLAB command as in Appendix A & B for the FFOA and FFOA respectively. The time to solution (t2s) and settling time (ts) are tabulated in Table 4.3

Table 4.3 The Settling Time and Time to Solution for mFFOA and FFOA

|  |  |  |  |  |
| --- | --- | --- | --- | --- |
| Runs |  | **mFFOA** | **FFOA** |  |
| ts (s) | t2s(s) | ts (s) | t2s(s) |
| 1 | 4.5227 | **126.6648** | **4.4551** | 126.9090 |
| 2 | **4.4695** | **125.3113** | 4.4920 | 126.30 |
| 3 | **4.4633** | **125.3536** | 4.5112 | 126.5801 |
| 4 | 4.4786 | **126.0660** | **4.4551** | 153.7282 |
| 5 | **4.4456** | **126.9538** | 4.4920 | 147.7347 |
| 6 | **4.4616** | **125.9995** | 4.5112 | 139.1311 |
| 7 | **4.4543** | **126.3670** | 4.4586 | 159.7811 |
| 8 | **4.4672** | **126.1129** | 4.6676 | 142.1975 |
| 9 | **4.4611** | **127.1459** | 4.6916 | 134.4642 |
| 10 | **4.4668** | 143.333 | 4.4764 | **140.7819** |

From Table 4.3 it is clear that the mFFOA has the least values (in bold) of settling time which is less than 5s in eight (8) runs, while FFOA obtained a value below that of the mFFOA in two test runs. Also in terms of time-to-solution the mFFOA obtained the optimized Q and R matrices within the least time (in bold) which is less than 150s in all the test run, except in the tenth run where the FFOA have a value below that of the mFFOA. This indicates the ability of the mFFOA to achieve fast control, since with any of the best values the PCS can achieve stability.

In order to test the efficiency of these optimized values on the PCS, the best value obtained using both algorithms is selected as follows:

For mFFOA and FFOA the best Q and R value that met the constraint (positive and semidefinite and positive definite matrices respectively) most were selected and given as:

*QmFFOA*

27.7918

  0.0163



 0.0588

0.0163

27.6817

0.0588

0.0588 

0.0588 



27.8825

*RmFFOA*  0.2898

17.4394 0 0 



*QFFOA*  0





 0

17.3370

0.0235

0.0235 

17.3230

*RFFOA*  0.4884

The optimized Q & R values are obtained within a time of 126.9538s when compared with the 140.7819s taken using the FFOA approach. The proposed method reduced the time taken by the FFOA by 13.8281s. These values are used to determine the gain (*K*) matrix as in equation (2.21) and the eigen values for the mFFOA and that of theFFOA method and

are given as follows.

*Km FFOA*  1.1404

# 9.5947

# 9.8054

*EmFFOA*

-114.5877

 - 2.2550

- 0.8568

*KFFOA*  0.4714

# 5.7896

5.9556

*EmFFOA*

- 69.8457

 - 2.2599

- 0.8519

It is shown above that the mFFOA obtained better result than the FFOA for the gain, and eigenvalues. The result is obtained using the MATLAB code in AppendixC.

In order to confirm the optimality of Q and R weighting matrices obtained from the modified fruit fly optimization algorithm (mFFOA), the responses of the PCS were plotted and superimposed with the best optimized values obtained using standard FFOA method. These response is presented in Fig 4.11. Notice that the blue lines show the responses

obtained for the LQR (mFFOA) and the redlines show the responses obtained for the LQR (FFOA).

### Response

**0.02**

**0**

**-0.02**

**mFFOA FFOA**

**(rad)**

**-0.04**

**-0.06**

**-0.08**

**0 1 2 3 4 5 6 7 8 9 10**

**Time(s)**

Fig 4.11: Step Response of PCS

As expected, the settling time (time taken for the PCS to stabilize) using LQR (mFFOA)andLQR (FFOA) nearly converged showing the convergence of the solution space using either of the approach. The advantage of the LQR mFFOA over the FFOA approach is that it saves cost in terms of time taken for the PCS to stabilize using LQR based mFFOA which is 4.4456s when compared with that taken using FFOA which is 4.4764s.

## CHAPTER FIVE CONCLUSION AND RECOMMENDATIONS

### Summary

This research has proposed a modified fruit fly optimization algorithm using decreasing inertial weight and adaptive search radius with decreasing iteration function, which was aimed at providing an efficient balance between exploration and exploitationand improved the rate at which the standard algorithm moves towards the global optimal. The performance of the algorithm was confirmed using ten optimization test function and the following findings were reported.

* + 1. The introduction of decreasing inertial weight (*w*) improved the poor exploration problem of the standard FFOA.
		2. The proposed algorithm determined efficiently the optimal values of linear quadratic regulator controllers weighting matrices (Q and R) with the least time when compared with the standard FFOA. This has helped in reducing cost in terms of time.
		3. The LQR controller stabilized the Pitch control system of an aircraft efficiently.

### Conclusion

Fruit Fly Optimization Algorithm (FFOA) is a class of evolutionary algorithmwhich was model based on the food finding behaviour of the fruitfly. In order to overcome the common problems (local optima and fixed search radius) associated with FFOA, a

modified version called the mFFOA has been developed, using, decreasinginertial weight and adaptive search radius with decreasing iteration function in MATLAB R2015a and the performance of the developed algorithms was evaluated using ten mathematical optimization test functions with diverse characteristics **(**Ackley, Alpine, Eggcrate, Griewank, Pathologic, Rastrigrin, Rosenbrock, Schaffer, Sphere, and Whitley**)**. The result obtained shows that mFFOA performed better than the standard FFOA with the Ackley and Whitely test functions there by indicating 20% improvement over the standard FFOA. This shows that the mFFOA has a better search radius and higher ability of escaping local optimal when compared with the standard FFOA. Also the proposed algorithm reduced the time taken by the FFOA to obtain the optimized Q and R matrices by 13.8281s. From the PCS step response analysis the result obtained demonstrated that the proposed algorithm can certainly stabilized the pitch control system within a settling time of 4.4456s. This is an indication of the validity of the mFFOA.

### Significant Contributions

A lot of research works have been done on improving the local optimal of Fruit Fly Optimization Algorithm. Many researches have also been conducted on different area of its application. The significant contributions of this research work are as follows:

* + 1. Development of a modified FFOA (mFFOA) with a decreasing inertial weight with particular emphasis on improving exploration capability of the standard FFOA.
		2. The optimized weighting matrices (Q and R) of the LQR based aircraft based PCSusing the mFFOA based approach were obtained in 126.954s as against

140.7819s when using the standard FFOA. This represents an improvement of 9.822% in time-to-solution.

* + 1. The Q and R values of the LQR obtained using the mFFOA based approach were able to settle the PCS in 4.4456s as compared to 4.4764s when the values from the standard FFOA based approach were used representing an improvement of 0.69%.

### Recommendation for Further Work

The following possible area is recommended for consideration for future research: Application of the developed model for optimal determination of the weighting matrices can be extended to other areas in power system control, stability analysis and motor speed control.

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## APPENDICES

## APPENDIX A

*function mFFOA*

*%\*\*\* Empty Memory clc*

*clear format long*

*%\*\*\* Random initial fruit fly swarm location X\_axis=10\*rand();*

*Y\_axis=10\*rand(); Radius=rand(1,2); Lamda\_min=min(Radius); Lamda\_max=max(Radius); Weight=rand(1,2); wmax=max(Weight); wmin=min(Weight);*

*%\*\*\* Set parameters*

*maxgen=500;%input('Provide the Maximum Generation:= '); % Iterations clc*

*sizepop=50;%input('Provide the Population of Fruit Flies:='); % Population size*

*%\*\*\* Optimization started, use the sense of smell to find food. clc*

*testfunction=0;%input('Choose:::\n0 to Determin Q&R Matrices\n1 to Run Ackley\n2 to Run Alpine\n3 to Run Eggcrate\n4 to Run Grienwangk\n5 to Pathologic\n6 to Run Rastrigin\n7 to Run Rosenbrock\n8 to Run Schaffer\n9 to Run Sphere\n10 to Run Whitely\n\n::=');*

*QR\_Iteration=ceil(maxgen/40); if testfunction ==0*

*A=[-2.02,1,0;-6.9868,-2.9476,0;0,1,0];%input('Please Enter The A*

*matrix:\n Such That:\n dx/dt=Ax(t)+Bu(t).\n\nA = '); clc*

*B=[0.16;11.7304;0];%input('Please Enter The B matrix:\n Such That:\n dx/dt=Ax(t)+Bu(t).\n\nB = ');*

*tic*

*end*

*clc t=0;*

*while t<QR\_Iteration [Q,R]=lqrQR(A,B)*

*t=t+1; end*

*if testfunction ~=0 ite=0;*

*for i=1:sizepop X(i)=X\_axis+2\*rand()-1; Y(i)=Y\_axis+2\*rand()-1;*

*%\*\*\*? Since the food location cannot be known, the distance to the origin is*

*% thus estimated first (Dist), then the smell concentration judgment value (S) is*

*% calculated, and this value is the reciprocal of distance. Lamda=Lamda\_max\*exp(log(Lamda\_min/Lamda\_max)\*(i/sizepop)); w=wmax-((wmax-wmin)/sizepop)\*i;*

*D(i)=Lamda.\*((X(i).^2+Y(i).^2)^0.5); S(i)=(1./D(i)).\*w;*

*%\*\*\* Substitute smell concentration judgment value (S) into smell*

*% concentration judgment function (or called Fitness function) so as to find the*

*% smell concentration (Smelli) of the individual location of the fruit fly.*

*Smell(i)=objfunc(testfunction,S(i));%sin(S(i))./S(i); end*

*%\*\*\* Find out the fruit fly with maximal smell concentration (finding the*

*% maximal value) among the fruit fly swarm. [bestSmell bestindex]=min(Smell);*

*%\*\*\* Keep the best smell concentration value and x, y coordinate , and at this*

*% moment, the fruit fly swarm will use vision to fly towards that location.*

*X\_axis=X(bestindex); Y\_axis=Y(bestindex); Smellbest=bestSmell;*

*%\*\*\* Iterative optimization start for g=1:maxgen*

*%\*\*\* Give the random direction and distance for the search of food using*

*% osphresis by an individual fruit fly. for i=1:sizepop*

*X(i)=X\_axis+2\*rand()-1; Y(i)=Y\_axis+2\*rand()-1;*

*%\*\*\*? Since the food location cannot be known, the distance to the origin is*

*% thus estimated first (Dist), then the smell concentration judgment value (S) is*

*% calculated, and this value is the reciprocal of distance. D(i)=(X(i).^2+Y(i).^2).^0.5;*

*S(i)=1./D(i);*

*%\*\*\* Substitute smell concentration judgment value (S) into smell*

*% concentration judgment function (or called Fitness function) so as to find the*

*% smell concentration (Smelli) of the individual location of the fruit fly.*

*Smell(i)=objfunc(testfunction,S(i));%Smell(i)=sin(S(i))./S(i); end*

*%\*\*\* Find out the fruit fly with maximal smell concentration (finding the*

*% maximal value) among the fruit fly swarm. [bestSmell bestindex]=min(Smell);*

*%\*\*\* Determine whether the smell concentration better than the previous*

*% iteration of the concentration, if yes then keep the best smell concentration*

*% value and x, y coordinate, and at this moment, the fruit fly swarm will use*

*% vision to fly towards that location. if bestSmell<Smellbest*

*end*

*X\_axis=X(bestindex); Y\_axis=Y(bestindex); Smellbest=bestSmell;*

*disp(sprintf('%8g %8g %8.4f',maxgen,bestindex,Smellbest));*

*%\*\*\* Each iteration the Smell optimal value, record to an array yy. yy(g)=Smellbest;*

*Xbest(g)=X\_axis; Ybest(g)=Y\_axis; end*

*%\*\*\*Draw smell concentration of each iteration figure(1)*

*yy' plot(yy,'b')*

*title('Optimization process','fontsize',12)*

*xlabel('Iteration Number','fontsize',12);ylabel('Smell','fontsize',12); figure(2)*

*plot(Xbest,Ybest,'b');*

*title('Fruit fly flying route','fontsize',14)*

*xlabel('X-axis','fontsize',12);ylabel('Y-axis','fontsize',12); end*

*toc end*

## APPENDIX B

*function FFOA*

*%\*\*\* Empty Memory clc*

*clear*

*%\*\*\* Random initial fruit fly swarm location X\_axis=10\*rand();*

*Y\_axis=10\*rand();*

*%\*\*\* Set parameters*

*maxgen=input('Provide the Maximum Generation:= '); % Iterations clc*

*sizepop=input('Provide the Population of Fruit Flies:='); % Population size*

*%\*\*\* Optimization started, use the sense of smell to find food. clc*

*testfunction=input('Choose:::\n0 to Determin Q&R Matrices\n1 to Run Ackley\n2 to Run Alpine\n3 to Run Eggcrate\n4 to Run Grienwangk\n5 to Pathologic\n6 to Run Rastrigin\n7 to Run Rosenbrock\n8 to Run Schaffer\n9 to Run Sphere\n10 to Run Whitely\n\n::=');*

*QR\_Iteration=ceil(maxgen/40); if testfunction ==0*

*A=input('Please Enter The A matrix:\n Such That:\n dx/dt=Ax(t)+Bu(t).\n\nA = ');*

*clc*

*B=input('Please Enter The B matrix:\n Such That:\n dx/dt=Ax(t)+Bu(t).\n\nB = ');*

*tic*

*end*

*clc t=0;*

*while t<QR\_Iteration [Q,R]=lqrQR(A,B)*

*t=t+1; end*

*if testfunction ~=0 ite=0;*

*for i=1:sizepop X(i)=X\_axis+2\*rand()-1; Y(i)=Y\_axis+2\*rand()-1;*

*%\*\*\*? Since the food location cannot be known, the distance to the origin is*

*% thus estimated first (Dist), then the smell concentration judgment value (S) is*

*% calculated, and this value is the reciprocal of distance. D(i)=(X(i).^2+Y(i).^2)^0.5;*

*S(i)=1./D(i);*

*%\*\*\* Substitute smell concentration judgment value (S) into smell*

*% concentration judgment function (or called Fitness function) so as to find the*

*% smell concentration (Smelli) of the individual location of the fruit fly.*

*Smell(i)=objfunc(testfunction,S(i));%sin(S(i))./S(i);*

*end*

*%\*\*\* Find out the fruit fly with maximal smell concentration (finding the*

*% maximal value) among the fruit fly swarm. [bestSmell bestindex]=min(Smell);*

*%\*\*\* Keep the best smell concentration value and x, y coordinate , and at this*

*% moment, the fruit fly swarm will use vision to fly towards that location.*

*X\_axis=X(bestindex); Y\_axis=Y(bestindex); Smellbest=bestSmell;*

*%\*\*\* Iterative optimization start for g=1:maxgen*

*%\*\*\* Give the random direction and distance for the search of food using*

*% osphresis by an individual fruit fly. for i=1:sizepop*

*X(i)=X\_axis+2\*rand()-1; Y(i)=Y\_axis+2\*rand()-1;*

*%\*\*\*? Since the food location cannot be known, the distance to the origin is*

*% thus estimated first (Dist), then the smell concentration judgment value (S) is*

*% calculated, and this value is the reciprocal of distance. D(i)=(X(i).^2+Y(i).^2).^0.5;*

*S(i)=1./D(i);*

*%\*\*\* Substitute smell concentration judgment value (S) into smell*

*% concentration judgment function (or called Fitness function) so as to find the*

*% smell concentration (Smelli) of the individual location of the fruit fly.*

*Smell(i)=objfunc(testfunction,S(i));%Smell(i)=sin(S(i))./S(i); end*

*%\*\*\* Find out the fruit fly with maximal smell concentration (finding the*

*% maximal value) among the fruit fly swarm. [bestSmell bestindex]=min(Smell);*

*%\*\*\* Determine whether the smell concentration better than the previous*

*% iteration of the concentration, if yes then keep the best smell concentration*

*% value and x, y coordinate , and at this moment, the fruit fly swarm will use*

*% vision to fly towards that location. if bestSmell<Smellbest*

*X\_axis=X(bestindex); Y\_axis=Y(bestindex); Smellbest=bestSmell;*

*end*

*disp(sprintf('%8g %8g %8.4f',maxgen,bestindex,Smellbest));*

*%\*\*\* Each iteration the Smell optimal value, record to an array yy. yy(g)=Smellbest;*

*Xbest(g)=X\_axis; Ybest(g)=Y\_axis; end*

*%\*\*\*Draw smell concentration of each iteration figure(1)*

*yy'*

*plot(yy,'-k')*

*title('Optimization process','fontsize',12)*

*xlabel('Iteration Number','fontsize',12);ylabel('Smell','fontsize',12); figure(2)*

*plot(Xbest,Ybest,'b.');*

*title('Fruit fly flying route','fontsize',14)*

*xlabel('X-axis','fontsize',12);ylabel('Y-axis','fontsize',12); end*

*toc end*

## APPENDIX C

*function xA= STEP\_RESPONSE clc*

*clear all A=inputA; B=inputB; C=inputC; D=inputD;*

*%Determin the Controllability and Observability of the system Mcr=ctrb(A,B);*

*Mob=obsv(A,C);*

*if rank(Mcr)==size(A) 'System is Controlable';*

*else*

*'System is NOT Controlable'*

*end CONTR\_RANK=rank(Mcr) if rank(Mob)==size(A)*

*'System is Observable' else*

*'System is NOT Observable'*

*end OBSV\_RANK=rank(Mob) Q\_mFOA=inputQ\_mFOA; R\_mFOA=inputR\_mFOA; Q\_FOA=inputQ\_FOA; R\_FOA=inputR\_FOA;*

*% Settings for mFOA.*

*[K\_mFOA P\_mFOA E\_mFOA]=lqr(A,B,Q\_mFOA,R\_mFOA)%Q and R used here are obtained from mFOA*

*sys\_LQ\_mFOA =ss(A-B\*K\_mFOA ,B,C,D); pzmap(sys\_LQ\_mFOA)*

*sgrid pause*

*x=[2;-0.04;0.02]; t=0:0.02:10;*

*x0=initial(sys\_LQ\_mFOA,x,t);*

*%ssize(x0);*

*%size(X1) X2mFOA=[1;0; 0;]\*x0';*

*% Settings for FOA.*

*[K\_FOA P\_FOA E\_FOA]=lqr(A,B,Q\_FOA,R\_FOA)%Q and R used here are obtained from FOA*

*sys\_LQ\_FOA=ss(A-B\*K\_FOA,B,C,D);*

*pzmap(sys\_LQ\_FOA) sgrid*

*pause*

*x=[2;-0.04;0.02]; t=0:0.02:10;*

*x0=initial(sys\_LQ\_FOA,x,t);*

*%size(X1) X2FOA=[0;1;0]\*x0';*

*% Setting for trial and error*

*Q=eye(size(A));*

*R=1;*

*[K1 P1 E1]=lqr(A,B,Q,R)*

*sys\_ss=ss(A-B\*K1,B,C,D); x00=initial(sys\_ss,x,t); X11=[1;0;0]\*x00'; plot(t,X2mFOA,'b',t,X2FOA,'r') xlabel('Time(s)') ylabel('Pitch (rad)')*

*legend ( 'mFFOA', 'FFOA') hold on*

*% mFOA\_Info=stepinfo(X2mFOA,t);*

*%plot(t,X2FOA,'r') hold on title('Response ') xlabel('Time(s)')*

*ylabel(' (rad)')*

*%legend ( 'mFFOA', 'FFOA') disp('mFFOA') stepinfo(sys\_LQ\_mFOA) disp('FFOA') stepinfo(sys\_LQ\_FOA)*